## Advanced Control Approach for Hybrid Systems Based on

## **Solid Oxide Fuel Cells**

M. L. Ferrari Thermochemical Power Group (TPG) Dipartimento di Macchine, Sistemi Energetici e Trasporti (DIME) Università di Genova, Italy

mario.ferrari@unige.it

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#### 8 Abstract

9 This paper shows a new advanced control approach for operations in hybrid systems 10 equipped with solid oxide fuel cell technology. This new tool, which combines feed-forward and 11 standard proportional-integral techniques, controls the system during load changes avoiding failures 12 and stress conditions detrimental to component life. This approach was selected to combine 13 simplicity and good control performance. Moreover, the new approach presented in this paper 14 eliminates the need for mass flow rate meters and other expensive probes, usually required for a 15 commercial plant. Compared to previous works, better performance is achieved in controlling fuel 16 cell temperature (maximum gradient significantly lower than 3 K/min), reducing the pressure gap 17 between cathode and anode sides (at least a 30% decrease during transient operations), and 18 generating a higher safe margin (at least a 10% increase) for the Steam-to-Carbon Ratio.

This new control system was developed and optimized using a hybrid system transient model implemented, validated and tested within previous works. The plant, comprising the coupling of a tubular solid oxide fuel cell stack with a microturbine, is equipped with a bypass valve able to connect the compressor outlet with the turbine inlet duct for rotational speed control. Following model development and tuning activities, several operative conditions were considered to show the new control system increased performance compared to previous tools (the same hybrid system model was used with the new control approach). Special attention was devoted to electrical load
steps and ramps considering significant changes in ambient conditions.

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#### 29 Keywords

30 Control system, SOFC hybrid system, feed-forward technique, PI controller.

#### 31 **1. Introduction**

Hybrid systems, consisting of a solid oxide fuel cell (SOFC) combined with a microturbine (mGT), are expected to have a significant role due to widespread distributed generation paradigm [1-4] and hydrogen economy [5-7]. More specifically, high performance aspects in small-size systems (ultra-high efficiency [8,9], ultra-low emissions [10], fuel flexibility [11,12] and cogenerative applications [13,14]) of these innovative plants are essential in terms of environmental and energy demand [15,16].

38 Despite the important results obtained for SOFC hybrid systems through both theoretical 39 [17-19] and experimental [8,20,21] tools, only one prototype, developed by Siemens-Westinghouse 40 [22], reached performance levels close to the expectations. This low rate of success for these kinds of plants is due to the high cost of components [7,23] and technical problems related to system 41 42 integration [7,24,25]. An important technical issue not completely settled concerns the control 43 system because SOFC hybrid plants are subject to several additional constraints as opposed to 44 standard mGT plants [26]. More specifically, in addition to turbine constraints (maximum rotational 45 speed, surge line and maximum thermal stress for components [27]), other risk situations must be 46 addressed [26,28], including (I) excessive temperature or (II) thermal gradient in the fuel cell, (III) 47 excessive pressure difference between cathodic and anodic sides and (IV) too low Steam-To-Carbon Ratio (STCR) in the SOFC anodic side. These constraints must be considered not only for 48 49 steady-state conditions, but also during time-dependent operations [29], such as load variations,

50 ambient temperature changes and start-up/shutdown phases [30]. More specifically, several 51 challenges must be overcome to couple the very fast response of the mGT system (low mechanical 52 inertia of the turbine shaft) with the slow thermal variations of the SOFC stack [31] (high thermal 53 capacitance of fuel cell materials), while the different volume values of SOFC sides generate 54 different time-dependent performance in terms of pressurization/depressurization delays (an 55 important aspect to take into account in order to prevent excessive cathode/anode pressure 56 difference during transient operations [25]). Moreover, the fluid dynamic and chemical responses of 57 the anodic side, important aspects to avoid low STCR values, are usually not in line with the 58 transient behaviour necessary to prevent other failures [32-34].

59 Although in the last ten years several works [29,33,35-37] have been carried out on these 60 control issues, the problem is not completely solved due to the large number of constraints to be 61 considered and aspects related to costs that have not been completely optimized. For instance, even 62 if some papers [33,36,37] presented effective control systems for SOFC hybrid plants, thermal 63 stress on the fuel cell was not always prevented (significant thermal gradient: higher than 3 K/min 64 [38] especially for large load steps) and expensive probes were used (e.g. mass flow rate meters in 65 [33,35]). Moreover, the cathode/anode pressure difference was carefully considered only in [33], 66 while other control systems showing interesting result neglected the constraints of this important 67 property (see [26] for experimental aspects). Also the time-dependent aspects related to anodic 68 recirculation were often neglected (considering constant recirculation ratios [38]) or based on very 69 simple approaches [37]. Since the importance of anodic circuit response is essential in preventing 70 failures (e.g. low STCR), it is imperative to develop a transient model of the anodic devices (e.g. an 71 anodic ejector [26,39]) to study a reliable control system for the entire plant [33].

This work focused on the development of an advanced control system for SOFC hybrid plants. So, the control strategy presented in [33] was improved considering the coupling of Proportional-Integral (PI) controllers with feed-forward approaches to prevent thermal stress in the fuel cell and to reduce the peak values of cathode/anode pressure difference and STCR. Since the 76 thermal capacitance of the stack is very high, the PI controller necessary to maintain constant stack 77 temperature must be a very slow response device (as done in [33]) to avoid unstable behaviour. 78 However, this approach cannot prevent significant thermal gradients (higher than 3 K/min) in the 79 fuel cell (responsible of serious stress on ceramic material) because the new rotational speed set-80 point is generated only after an excessive temperature oscillation. On the other hand, the coupling 81 with feed-forward technique (in a system equipped with load variation smoothing devices: a battery 82 package or an electrical grid) can obtain the new rotational speed with the requested time 83 performance and without instability problems. Moreover, this is a simple approach (in comparison 84 with multiple-input and multiple-output controllers), which can combine possible corrective actions for disturbances (e.g. variations of ambient conditions) with less oscillations in plant critical 85 properties. Even if the same basis shown in [33] was maintained (e.g. the mGT speed control was 86 carried out with a compressor/turbine bypass valve), the results obtained with a Matlab<sup>®</sup>-Simulink<sup>®</sup> 87 88 transient model shows better performance in terms of thermal and mechanical stress on the components. The Matlab<sup>®</sup> version used in this work is the R2010a (7.10.0.499), which is coupled 89 with version 7.5 of the Simulink<sup> $\mathbb{R}$ </sup> tool. 90

91 This work demonstrates improved control performance, over previous works [29,32,33,41], 92 which can prevent failures and increase component life, also broadening the types of transient 93 operations (e.g. variations of ambient conditions) carried out with a previously validated model 94 [42,43].

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### 2. Plant Layout and Control System

The hybrid system considered in this work (continuous lines in Fig.1) is based on Siemens-Westinghouse [22,33] technology for a global size in the range of 300 kW. The plant layout comprises the coupling of a tubular pressurized SOFC with a recuperated microturbine. On the cathodic side air is compressed by a radial machine, preheated by the recuperator and fed to the fuel cell, while in the anodic ducts fuel (methane) is converted into a hydrogen rich mixture by a

101 reformer unit located upstream of the stack. The anodic side is based on a recirculation system 102 carried out by a single-stage ejector: methane is pre-heated with the plant exhaust flow and fed into 103 the ejector primary duct, while a part of the SOFC exhaust (anodic flow) is recirculated by the 104 ejector (secondary nozzle). The flow comprising the mixture of this recirculation and methane is fed 105 to the stack anodic side. Finally, the anodic circuit outlet flow is mixed with the cathodic exhaust 106 flow in the off-gas burner to increase turbine inlet enthalpy. The expander can produce the power needed for the compressor and an useful power additional to the fuel cell generation. On the 107 108 electrical side the system is equipped with a battery package in case of stand-alone operation mode 109 (in case of grid connected operations, the electrical grid can substitute the battery function). The 110 main property values of the plant at design conditions are reported in Tab.1.

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Table 1. Design values of main plant properties.

| Net electrical power of the entire hybrid system [kW]  | 284.8  |
|--|--------|
| Stack electrical power [kW]                            | 231.3  |
| Net electrical power of the turbine [kW]               | 53.5   |
| Power consumed by the fuel compressor [kW]             | 9.4    |
| Global net electrical efficiency [-]                   | 0.637  |
| Fuel utilization factor                                | 0.85   |
| Current density [mA/cm <sup>2</sup> ]                  | 423.9  |
| Stack average temperature [K]                          | 1229.8 |
| Fuel mass flow rate in the ejector primary duct [kg/s] | 0.009  |
| Anodic ejector recirculation ratio [-]                 | 7.18   |
| Air mass flow rate [kg/s]                              | 0.658  |
| Compression ratio [-]                                  | 3.85   |
| Recuperator effectiveness [-]                          | 0.89   |
| Turbine inlet temperature [K]                          | 1080.1 |
| Turbine outlet temperature [K]                         | 847.6  |
| Shaft rotational speed [rpm]                           | 68000  |

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The control strategy considered in this work is shown in Fig.1 using dotted lines. It is based on the coupling of standard PI controllers (as in [33]) with a feed-forward technique. The latter approach is necessary to prevent the high thermal gradient values shown in [33] and in other previous works (e.g. in [38]). Since the stack thermal capacitance is very high, a possible simple 118 solution to avoid temperature oscillations (and thermal gradients higher than 3 K/min) is the 119 application of the feed-forward technique (based on interpolation tables) because it can obtain the 120 requested rotational speed change without the unstable behaviour typical of a feedback-based 121 controller. However, this new approach can produce the expected performance if load variation is 122 smoothed by a battery or an electrical grid. The numbers of control lines is selected in accordance 123 with [33]. For this reason, where this new approach allows removing a control line in comparison with [33], the related number is not used. This layout is based on a bypass valve for direct 124 125 connection between the compressor outlet and the turbine inlet ducts. This approach (proposed in 126 [33]) is necessary to control the mGT rotational speed (point 1 in Fig.1) solving the issue related to 127 the difference between the small mechanical inertia of the microturbine shaft and the very high 128 thermal capacitance of the fuel cell stack. While the fractional opening (FO) design value is low 129 (0.05) to achieve good efficiency in steady-state conditions, this value is managed by a PI controller 130 to maintain the mGT rotational speed at its set-point value.

131 The system input is the power demand (point 2) for the entire plant. The actual power 132 requirement is calculated considering a control device capable of smoothing the input variations 133 with a battery package as in Fig.1 or through the electrical grid. Also in this work the electrical 134 dumper is controlled by a PI equipped with a previous step block (see Fig.2 for details) capable of 135 reducing power change effects; different solutions are available. The coefficient of the integral part 136 of this PI is calculated through an interpolation table on the basis of the bypass valve FO (this 137 approach is necessary to reduce fuel cell pressure difference by decreasing the response speed of 138 power variation smoothing when FO is significantly different from its design value). Then, the 139 power requested to the SOFC is calculated by multiplying the input signal by a sharing-out 140 coefficient (point 3) as presented in [33]. However, unlike [33], an initial improvement is obtained 141 through a feed-forward approach used to evaluate this coefficient to keep the bypass valve set-point 142 value at 0.05. Instead of a slow response PI controller [33] being responsible for a very significant FO oscillation (linked with a cathode/anode pressure difference high peak), a table of data coming 143

144 from steady-state analysis is interpolated on the basis of the hybrid system power demand, ambient 145 conditions, anodic recirculation temperature and fuel temperature. The SOFC power demand (point 146 5) is used to evaluate stack current (point 7) calculated by a fast response PI controller. This control 147 device operates to nullify the difference between the SOFC power demand and the effective power 148 generated by the fuel cell (point 6). The remaining electrical demand (point 8) is satisfied by the 149 mGT generator. Fuel flow rate is managed by a valve located upstream of the ejector primary ducts 150 whose FO value (point 12) is calculated through a second feed-forward controller (a second table of 151 data interpolated on the basis of the hybrid system power demand, ambient conditions, anodic 152 recirculation temperature and fuel temperature), instead of a PI device as carried out in [33]. With 153 this new approach, it is possible to keep constant (0.85 at off-design conditions) the fuel utilization 154 factor inside the SOFC, avoiding an expensive fuel mass flow rate probe (necessary device to 155 operate as in [33] with a slow-response PI). Moreover, this second feed-forward controller can 156 significantly reduce the fuel utilization factor oscillations in comparison to the results obtained in 157 [33]. A final controller is necessary to maintain constant SOFC average temperature value. Also in 158 this case, a feed-forward approach is used to calculate the rotational speed set-point (point 11), 159 replacing the slow response PI controller proposed in [33]. This control type change is necessary to 160 avoid significant oscillations in SOFC average temperature, which can generate dangerous thermal 161 stress on ceramic material (especially with thermal gradient values higher than 3 K/min [40]). To 162 ensure the flexibility needed to achieve the response of this controller, the table of data interpolation 163 (including the effects of ambient condition, anodic recirculation temperature and fuel temperature) 164 is carried out including a delay for the hybrid system power demand. This delay unit is based on a 165 slow-response PI controller where the plant power demand is operated as a set-point and the 166 controller output is used as a feedback signal input (see Fig.2 for details). The complete diagram of 167 a PI controller coupled with a previous step block is shown in Fig.2. This configuration can operate 168 as a delay (including the proportional part) of the input value because the previous step block 169 generates the PI set-point value equal to the PI output calculated during the previous calculation

170 step. It also includes an optional input line that is used when it is necessary to change the integral 171 part coefficient. At steady-state condition the output value converges with the input value. This 172 solution was selected instead of a transfer function to utilize similar control devices within the 173 system, thus simplifying the approach: just PI controllers, interpolation tables and algebraic blocks. 174 However, the same effect can be obtained with a first-order transfer function.

175 The values implemented in the interpolation tables shown in Fig.1 were obtained by steadystate calculations carried out considering different values in plant power demand and other 176 177 influence properties (the main results of this steady-state analysis was reported in [44]) or (for the 178 coefficient factors related to the PI integral part for battery management) from preliminary 179 simulations. The typical limitation of the feed-forward approach (no corrective actions from 180 disturbances) was solved including interpolation table variation (with apt corrective factors) in case 181 of variations of measurable disturbances (ambient conditions, fuel temperature and fuel 182 composition). For this reason Fig.1 includes the following inputs: ambient conditions (temperature, 183 pressure and humidity), fuel temperature and anodic recirculation temperature (its variation can 184 show the effect of fuel composition variation to be compensated in the interpolation tables). 185 Moreover, the not measurable disturbances (e.g. degradation of plant components) can also be 186 compensated with the same approach. In this case, it is necessary to use available measurements to 187 detect the degradation (and the degradation level). For instance, the stack degradation can also be 188 detected by anodic recirculation temperature. In this case, feed-forward components can be adapted 189 modifying the interpolation tables on the basis of this property, maintaining, also in case of stack 190 degradation the target temperature value of the SOFC.

#### 191 **3. Model**

192 The control system development and testing were carried out with a transient model 193 implemented in Matlab<sup>®</sup>-Simulink<sup>®</sup> environment. Although in this work the control system is 194 completely new, the same models of [33] were considered for plant components to highlight the 195 good performance achieved by this new control system compared to the previous one [33]. This 196 model was developed using the TRANSEO tool [45,46], a visual, user-friendly modular program 197 based on a library of components for off-design, transient and dynamic analyses [47] of energy 198 systems.

199 The modelling technique for the main part of the plant components is based on a 0-D 200 approach (balance equations integrated just between inlet and outlet of devices) called "lumped 201 volume". Each component (except the recuperator that is based on a quasi-2-D technique [47]) is 202 modelled with an off-design calculation software connected to a constant section pipe model for 203 fluid dynamic delay [44]. This simplified approach is essential to reach reasonable computational 204 time, ensuring that calculation performance is satisfactory for plant level simulations, as 205 demonstrated in several previous validation works carried out with this modelling technique 206 [42,43]. More specifically, 0-D approaches were demonstrated [19,32,33] to be very effective in 207 control system development and assessment. As stressed in [33,45], models of all plant components 208 include thermal loss and transient response related to changes in chemical composition.

#### 209 3.1 <u>Fuel Cell Model</u>

210 This paper is based on a fuel cell tubular geometry, similar to the design proposed in 211 [33,45], and on surrounding facilities (reformer, pre-heating tube, anodic recirculation, etc.) 212 connected as presented in [49]. The fuel cell model is based on the following hypotheses: adiabatic, 213 uniform voltage, chemical reactions at equilibrium, CO electrochemical reaction neglected. As 214 presented in [50], the fuel cell model includes: voltage calculation subtracting ohmic and activation 215 losses from Nernst's potential, equilibrium of reforming and shifting chemical reactions, mass 216 balances of anodic and cathodic flows (including the effect of reactions), energy balances of flows 217 (this calculation includes: the anodic gas, the flow within the pre-heating quartz tube and the 218 cathodic air, the energy balance related to the tube and the solid PEN (positive(P)-electrolyte(E)-219 negative(N)) structure. A time-dependent first-order differential equation is used to calculate the stack material average temperature considering thermal balances and the total stack thermal capacitance.

# This model was validated at stack level considering a wide result comparison against a detailed 1-D model (previously validated against experiments) in both steady-state and transient conditions [50]. The assessment presented in [50] showed that the 0-D approach used for the fuel cell model can generate reliable results for plant level analysis and control system development.

#### 226 3.3 <u>Models for Plant Components</u>

227 Special attention was devoted to the ejector transient model. It was developed in previous 228 works [42,45,46] and validated against experimental data at both steady-state and transient 229 conditions [42]. Given the importance of this component for the anodic side performance [51-53], a 230 detailed validation was carried out for recirculation systems using experimental data obtained 231 through reduced-scale emulator rigs [42,54].

Models for the compressor and turbine are based on the interpolation of characteristic nondimensional curves. Although this is a typical approach for these kinds of machines [55-57], several previous works [45-48] carried out with TRANSEO tool validated these models in transient operations too. The recuperator model is based on a quasi-2D approach to achieve reliable results. Previous works [46,48,58] demonstrated that this technique based on 10 calculation nodes is a good compromise between result performance and computational time. Moreover, the recuperator model was validated against experimental data in [48,58].

Finally, validation activity was carried out at system level using the hybrid system emulator rig of the NETL - U.S. DOE located in Morgantown (WV). This plant was able to validate all the cathodic-side models (compressor, turbine, shaft, generator, recuperator, cathodic volume and offgas burner) at both steady-state and transient conditions [43].

#### 243 **4. Results**

To compare the performance obtained with this new control system to the results obtained in [33], initial simulation tests were carried out considering a 10% load step decrease and a 5% load step increase. In both cases, the same hybrid system model shown in [33] was used to perform a control system comparison. Then, the new control system was used to analyse the effect of changes in ambient conditions in conjunction with electrical load ramps (to simulate real plant operations).

#### 249 4.1. Load Step Decrease

250 This paragraph presents a simulation carried out with the model using the new advanced 251 control system based on the interpolation tables shown in Fig.1: a feed-forward (FF) approach is 252 implemented for some controllers. To compare the results to the performance obtained with a 253 previous PI based control system [33], a 10% load step was considered (as in [33]) for the entire 254 hybrid plant: from about 284.8 kW to 256.3 kW at constant ambient conditions (air at 60% relative 255 humidity, 288.15 K temperature and 1.013 bar pressure). Many simulations were carried out before 256 obtaining the results presented here. This preliminary work was necessary to implement the 257 parameter values especially for the coefficient table of the battery PI controller and for the response 258 of the rotational speed set-point calculator. The results shown in [33] (for PI coefficients coming 259 from Ziegler-Nichols technique [59] followed by a significant tuning activity) were a starting point 260 to maintain the controller in stable condition. However, in this work, extensive activity based on 261 trial-and-error technique was carried out to improve results. More specifically, it was very difficult 262 to synchronize the very different dynamics of the following parameters: fuel cell load, turbine 263 rotational speed and fuel mass flow rate. For instance, to maintain constant SOFC average 264 temperature (with maximum gradient lower than 3 K/min) it is necessary to adapt turbine rotational 265 speed as quickly as load changes on the stack. However, a strong limitation is present to avoid an 266 excessive large bypass valve (decreasing plant efficiency) or surge problems. For this reason, high 267 temperature gradients were not prevented in [33,38]. Moreover, the different anodic loop dynamics

(mainly due to the different volumes of the cell sides) can generate excessively high differential 268 269 pressure values if fuel flow rate is not changed with the same time scales. Unfortunately, if this 270 mass flow rate variation is carried out too quickly (especially in case of load increase) the constraint 271 related to the STCR parameter is not satisfied, generating values lower than 1.8 during the transient 272 operations. So, the battery controller was tuned to obtain the fastest possible response and to reach a 273 compromise between battery operation time decrease (linked with cost decrease due to limited 274 installation of battery components due to maximum power decrease requested by this component) 275 and system, operated in accordance with the various constraints (including the SOFC time-276 dependent thermal gradient constraint, usually neglected in several previous works [38]).

277 The global management of the plant obtained with the control system is shown in Fig.3. 278 Since the electrical demand (for the whole hybrid system) is decreased by the 10% step at time 0 of 279 Fig.3, the battery package is used to smooth this load decrease: both SOFC and mGT can slowly reduce slowly their load values, while the additional power produced by the plant is absorbed by the 280 281 battery (negative power means battery re-charging phase). However, if the plant can be connected 282 to an external electrical grid, the same behaviour (same power variation smoothing) can be obtained 283 without battery costs. Since the battery smoothing effect has a time response longer than the thermal 284 one (mainly due to the SOFC high thermal capacitance), the effect of fluid dynamic response (also 285 including pressurization/depressurization volume response) is negligible in the results presented in 286 this work. Furthermore, as shown in Fig.4, the rotational speed oscillation typical of load step 287 response (as shown in [33]) is also not present because load demand variation on the mGT is 288 smoothed by the battery. Figure 4 also includes fuel cell inlet pressure at the cathodic side 289 (downstream of the air pre-heating tube) showing a pressure decrease trend due to rotational speed 290 decrease. These trends, compared to the results obtained in [33] (see Fig.4), show a slow-response 291 decrease due to a slow decrease in rotational speed set-point (signal 11 in Fig.1) driven by the PI 292 connected to a previous step block. This approach is necessary to produce a proper delayed response to keep constant the SOFC temperature (Fig.5). The good performance of this controlling 293

solution is well demonstrated by Fig.5 because SOFC average temperature is maintained almost constant (0.7 K maximum variation during this test) and time-dependent temperature gradient is almost negligible. The load change smoothing obtained using the battery and the good rotational speed set-point calculation carried out through the feed-forward (FF) approach can avoid significant SOFC temperature oscillations. This is a significant improvement considering that the previous solution [33] based on a PI controller generated a high temperature maximum gradient (about 10 K/min) usually not sustainable by the fuel cell stack.

301 During the test, the sharing-out coefficient (Fig.6) and the fractional opening (Fig.7) of the 302 bypass valve show decreased oscillating behaviour and a slower response variation compared to the 303 results reported in [33]. Also their trends are due to the battery smoothing effect coupled with a 304 feed-forward approach for the sharing-out coefficient calculation too. Using the interpolation table 305 (instead of the PI controller shown in [33]) to calculate this coefficient value is an effective solution to maintain the 0.05 fractional opening value at steady-state condition, avoiding efficiency (defined 306 in Eq.1) decay due to high mass flow rate bypassed from compressor to turbine. The good 307 308 performance obtained with this new control system is shown by the plant net efficiency (Fig.8). In 309 comparison with results calculated in [33], it is possible to avoid significant efficiency decays at 310 transient condition too.

311 
$$eff = \frac{P_{FC} + P_{mGT} - P_{aux}}{m_{fuel} \cdot LHV}$$
(1)

312 
$$U_{f} = \frac{\left[n(H_{2}) + 4 \cdot n(CH_{4}) + n(CO)\right]_{FC_{in}} - \left[n(H_{2}) + 4 \cdot n(CH_{4}) + n(CO)\right]_{FC_{out}}}{\left[n(H_{2}) + 4 \cdot n(CH_{4}) + n(CO)\right]_{FC_{in}}}$$
(2)

The performance obtained with the interpolation table needed to manage the fuel valve is reported in Fig.9. Both current and fuel mass flow rate decreases are slower in comparison with previous results [33] because the battery can smooth the load change on the fuel cell. This approach allows maintaining almost constant fuel utilization value (see Eq.2 for its definition) with 1% maximum decay during the transient response (reaching the 0.85 design value at steady-state

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318 condition). This behaviour is significantly different from the results discussed in [33] where a 17%319 U<sub>f</sub> decay is shown immediately after the 10% load decrease step.

320 As mentioned in the Introduction, an effective control system for hybrid plants must be able 321 to prevent critical values also for the following parameters: STCR, anode-cathode differential 322 pressure, Turbine Inlet Temperature (TIT) and compressor surge margin. Even if it is very difficult 323 to maintain all these parameters within the constraints during time-dependent operations, the 324 smoothing effect of the battery coupled with the feed-forward technique can produce the requested 325 performance. So, the new control approach presented in this paper compensates for the different 326 dynamics responsible for possible critical conditions during transient operations. More specifically, Fig.10 shows that this new control system can prevent low STCR (see Eq.3) values and non-327 328 sustainable fuel cell differential pressure. In comparison with results shown in [33], it is possible to 329 obtain smaller variations increasing the possible plant operation field (larger load steps are acceptable) and to reduce mechanical stress on the stack. The maximum peak of differential 330 331 pressure value is significantly reduced (maximum peak absolute value from 17.6 mbar to 9.4 mbar) 332 using this new control system based on interpolation tables (feed-forward approach for three 333 parameters). For the other critical properties (TIT and Kp), Fig.11 shows that this new control 334 system can prevent TIT peaks and surge conditions. In comparison with [33], the behaviour is less 335 oscillating also for TIT and surge margin (see Eq.4 for its definition). However, no significant 336 thermal stress is generated by this load step (larger steps can be acceptable) because the TIT design 337 value has a significant safety margin (higher than 100 K for standard commercial mGTs) and the 338 temperature increase shown in Fig.11 is very small (about 5 K). Moreover, surge risk is prevented 339 because Kp parameter significantly increases in comparison with its design value.

340 
$$STCR = \frac{n(H_2O)}{n(CO) + n(CH_4)}$$
 (3)

341 
$$Kp = \frac{\beta_{s.l.} \cdot m}{\beta \cdot m_{s.l.}}$$
(4)

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342 Another important aspect to check in these kinds of plants is chemical stress on the fuel cell 343 due to significant chemical composition variation. For this reason, Fig.12 shows mass fractions of 344 the anodic outlet flow (upstream of the off-gas burner) referenced to their design values (each mass 345 fraction is divided by its design value to better show the time-depended variation). The design values are: 0.518 for CO<sub>2</sub>, 0.004 for H<sub>2</sub>, 0.438 for H<sub>2</sub>O and 0.040 for CO. To better present the 346 performance obtained with this new control system, attention is focused (Fig.12) on the results 347 348 obtained with the feed-forward (FF) approach. The chemical composition variation was maintained 349 fairly constant because the variations of mass fractions were always lower than 5%. Moreover, for 350 the most significant components (CO<sub>2</sub> and H<sub>2</sub>) in the flow, Fig.12 shows a variation lower than 351 0.4%. Similar stable performance was obtained on the cathodic side (with a plot not shown here for 352 sake of brevity).

353 To complete the evaluation of this new control system performance, the same simulation 354 (10% load step decrease) was carried out removing the battery (or the connection to an electrical 355 grid) from the system. In comparison with [33] (based on just feedback technique for all the 356 controllers), the results obtained in this case showed a better control of SOFC average temperature 357 (4 K oscillation instead of 29 K obtained in [33]) for the application of the feed-forward approach. 358 However, some parameters are significantly critical: anode-cathode differential pressure reached 77 359 mbar at the beginning of this transient operation, STCR showed an excessively large oscillation 360 (from 2.23 to 3.44) with possible risk values (lower than 1.8) increasing the load, and also an 361 important oscillation in surge margin (possible risks in other transient phases). So, even if the 362 coupling of PI controllers with a feed-forward approach can produce interesting results, the correct 363 behaviour of the plant (preventing risks) is obtained when a smoothing device is connected on the 364 electrical side (a battery or connection to an external grid), as shown in Fig.1.

365 4.2. Load Step Increase

366 A second transient response tested with this new control system is a load step increase. To carry out a comparison with the previous control approach proposed in [33], a 5% step increase was 367 368 considered starting from about 256.3 kW hybrid system load (90% of design value). At time 0, the electrical demand was increased with a step to about 270.6 kW (95% of design value) and the 369 370 simulation was completed when system reached a new steady-state condition. As shown in [33], 371 feedback-based controlling approaches cannot prevent temperature increase peaks because the 372 rotational speed set-point increase is obtained with a measured temperature (in [33] anodic 373 recirculation temperature was used) higher than the set-point. In case this variation is significant (in 374 Fig.13 the PI approach shows a 13.6 K increase), the stack can be damaged (if maximum 375 temperature constraints is exceeded) also at low thermal gradients conditions. On the other hand, a 376 feed-forward approach can produce the necessary coupling between fuel cell load and machine 377 rotational speed especially if a battery is used to smooth effects related to load changes. For these 378 reasons, Fig.13 shows that this new control system can maintain constant SOFC average 379 temperature (Fig.13) also during load step increases avoiding risks due to temperature peaks and 380 stress related to high thermal gradient (always lower than 0.1 K/min with the FF control approach). 381 While results reported in [33] showed a temperature increase which forces to operate the cell with a 382 significant temperature safe margin (from the maximum), Fig.13 shows an almost constant trend 383 obtained with the new approach. Moreover, all the critical parameters were maintained by the 384 control system inside safe ranges. In details, STCR minimum value is 2.08 with a significant 385 margin from 1.8 [60], anode-cathode differential pressure has a -8.4 mbar peak, TIT shows a peak 386 at 1092 K maintaining a significant margin from the mGT maximum sustainable value, surge 387 margin decreases with a minimum value of 1.107 that is higher than the design one.

#### 388 4.3. <u>Ramps for Load and Ambient Conditions</u>

In this final calculation the control system was tested with ramps for ambient conditions (temperature, pressure and humidity) and electrical load considering one hour and a half (5400 seconds). In details, conditions typical of morning operations were reproduced (one new value at the end of every 900 s periods connected with a linear trend): significant temperature and load demand increase (see Fig.14). The other properties (pressure and relative humidity) were managed simulating a good weather morning (Fig.14).

395 The power values obtained with the model (Fig.15) focus the attention on battery 396 performance, necessary to have this smooth behaviour. During this load increase ramp battery is 397 discharged to satisfy load demand with peaks (up to 14.7 kW). Other results show that this new 398 control system is able to manage the plant avoiding stress and risk conditions. For instance, Fig.16 399 shows that fuel cell average temperature is maintained almost constant ( $\pm 1.3$  K maximum variation) 400 with a rotational speed increase (from 58234 rpm to 64961 rpm) avoiding high thermal gradients 401 (maximum values less than 0.3 K/min). The other critical properties were maintained inside safe 402 range conditions. For instance, Fig.17 shows that STCR is always higher than 2.6 (significant safe 403 margin from 1.8 [60]) and maximum anode-cathode differential pressure is lower than 10 mbar 404 (considering its absolute value). Moreover, also the other properties, not reported here for sake of 405 brevity, were well controlled inside safe conditions. For instance, TIT maximum peak is about 1100 406 K (significant safety margin from its maximum value) and Kp is always higher than 1.1 (1.13) 407 minimum value during the test).

#### 408 **5.** Conclusions

This work is related to the development and testing of a new advanced control system for hybrid plants with pressurized SOFCs. Even if the calculations are presented considering a standalone application, the same approach can be used for grid connected systems where the battery operations are substituted by the electrical grid. The control logic is based on the coupling of PI controllers with feed-forward approaches necessary to avoid significant temperature variation in the cell (responsible of thermal stress problems) and to reduce the peak values of cathode/anode pressure difference and STCR. So, this work is able to demonstrate improved controlling performance for SOFC hybrid systems, in comparison with previous works [29,32,33,41]. In details, the same component models of [33] were used to compare the good performance obtained with this new controller with the results obtained with the old one shown in [33]. The main conclusions and results presented in this paper are:

This new control strategy is able to improve SOFC temperature management because it is
able to maintain almost constant this property, avoiding significant thermal gradients (maximum
values lower than 0.2 K/min for a 10% load step decrease).

The results obtained with the model show that anode-cathode differential pressure can be
maintained at sustainable values during transient operations too (maximum values lower than 10
mbar for a 10% load step decrease).

This new control system can keep all the critical properties inside safe conditions. STCR,
turbine TIT and Kp are always calculated with a significant safety margin from critical values. For
instance, STCR minimum value is 2.18 in the 10% load step decrease, while its limit value is
usually 1.8 [60].

• The tests carried out considering ramp variations in load and ambient conditions proved that 431 typical plant operations can be tolerated by this new advanced control system with good 432 performance (ramp test main results: thermal gradient in the cell lower than 0.3 K/min, anode-433 cathode differential pressure lower than 10 mbar, STCR minimum value higher than 2.05).

Additional activities are being developed at TPG on hybrid system controllers. More specifically, an emulator plant [61] is being operated to test control approaches in hardware-in-theloop configuration, considering not only traditional approaches, but also innovative ones (e.g. model predictive control logics [62], which is considered promising in co-generative plants [63]).

## 439 Acknowledgements

- 440 The author would like to thank Prof. Aristide F. Massardo, TPG Coordinator, for his essential
- scientific support and Prof. Alberto Traverso, the main developer of TRANSEO tool.

442

#### 443 Nomenclature

| Acronyms           |  |
|--------------------|--|
| AC                 | Ambient Conditions                               |
| DOE                | Department Of Energy                             |
| DS                 | DeSulfurizer                                     |
| FC                 | Fuel Cell  |
| FF                 | Feed-Forward                                     |
| HS                 | Hybrid System                                    |
| mGT                | micro Gas Turbine                                |
| NETL               | National Energy Technology Laboratory            |
| PI                 | Proportional-Integral controller                 |
| REC                | RECuperator                                      |
| SOFC               | Solid Oxide Fuel Cell                            |
| TPG                | Thermochemical Power Group                       |
| Variables          |  |
| Coeff              | power sharing-out coefficient [-]                |
| diff_p             | anode-cathode differential pressure [Pa]         |
| eff                | plant net efficiency [-]                         |
| FO                 | valve Fractional Opening [-]                     |
| LHV                | Low Heating Value [J/kg]                         |
| Кр                 | surge margin [-]                                 |
| K <sub>p</sub>     | proportional coefficient for a PI controller [-] |
| i                  | electrical current density [A/m <sup>2</sup> ]   |
| m                  | mass flow rate [kg/s]                            |
| n                  | molar flow rate [mol/s]                          |
| Ν                  | rotational speed [rpm]                           |
| р                  | pressure [Pa]                                    |
| Р                  | power [W]  |
| RH                 | Relative Humidity [%]                            |
| STCR               | Steam-To-Carbon Ratio [-]                        |
| Т                  | temperature [K]                                  |
| Та                 | ambient temperature [K]                          |
| TIT                | Turbine Inlet Temperature [K]                    |
| $U_{f}$            | fuel utilization factor [-]                      |
| XMA                | mass fraction [-]                                |
| Greek symbols      | S  |
| β                  | compression ratio                                |
| $	au_{\mathrm{I}}$ | integral coefficient for a PI controller [-]     |
| Subscripts         |  |
| ar                 | anodic recirculation                             |
| aux                | auxiliaries                                      |

| 444 | cath<br>dp<br>f<br>FC<br>in<br>mGT<br>out<br>s.l. | cathodic<br>design point<br>fuel<br>Fuel Cell<br>inlet<br>micro Gas Turbine<br>outlet<br>surge line |  |  |
|-----|---|---|--|--|
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#### **Figures and Tables**























compared to previous results [33].





(between anode and cathode sides).

Figure 17. Ramps for load and ambient conditions: fuel cell STCR and fuel cell differential pressure

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