

Geant4: a Game Changer in High Energy Physics and Related Applicative Fields

Tullio Basaglia^{a,1}, Zane W. Bell^b, Daniele D'Agostino^{c,d,*}, Paul V. Dressendorfer^b,
Simone Giani^a, Maria Grazia Pia^d, Paolo Saracco^d

^aEuropean Organization for Nuclear Research (CERN), Geneva, CH-1211 Geneva 23, Switzerland

^bIEEE, 445 Hoes Lane, Piscataway, NJ 08854, USA

^cDepartment of Informatics, Bioengineering, Robotics and Systems Engineering (DIBRIS), Università degli Studi di Genova, Via Dodecaneso 35, Genova, Italy

^dIstituto Nazionale di Fisica Nucleare (INFN), Sezione di Genova, Via Dodecaneso 33, Genova, Italy

Abstract

Geant4 is an object-oriented toolkit for the simulation of the passage of particles through matter. Its development was initially motivated by the requirements of physics experiments at high energy hadron colliders under construction in the last decade of the 20th century. Since its release in 1998, it has been exploited in many different applicative fields, including space science, nuclear physics, medical physics and archaeology. Its valuable support to scientific discovery is demonstrated by more than 16000 citations received in the past 25 years, including notable citations for main discoveries in different fields. This accomplishment shows that well designed software plays a key role in enabling scientific advancement. In this paper we discuss the key principles and the innovative decisions at the basis of Geant4, which made it a game changer in high energy physics and related fields, and outline some considerations regarding future directions.

Keywords: High Energy Physics, Software Engineering, C++; Monte Carlo, Geant4

1. Introduction

Geant4 [1–3] is an open source, object-oriented software toolkit for the simulation of the interactions of particles with matter. Its development was driven by the requirements of high energy physics experiments at large scale particle accelerators under construction in the last decade of the 20th century. Twenty-five years since its first public release, it is still actively maintained and widely used in a variety of domains for scientific research, for engineering and industrial tasks, for medical applications and for investigations of cultural heritage.

The success of Geant4 at enabling scientific discoveries and supporting technological advancements is demonstrated by the large number of citations of its main reference [1] and of patents based on it. These achievements are rooted in the software engineering grounds that shaped Geant4 conception, design and development.

This paper summarizes Geant4 main characteristics, documents Geant4's contribution to multidisciplinary scientific results over the past 25 years, reviews the role of software engineering at supporting them and discusses some future perspectives in the field. The focus is on showing that the grounds of Geant4's success and long life without any major structural update have been careful design, based on the exploitation of modern software engineering techniques, the adoption of the object-oriented methodology, and an early decision to use the C++ language, which in 1994, at the time when Geant4 development started, represented a brave decision.

Thanks to these choices, the software represented a game-changing factor that has shaped research work practice and has enabled scientific progress not only in high energy physics, where it contributed to the discovery of the Higgs boson [4, 5], but also in several other research fields.

The paper is structured as follows. Section 2 presents Geant4 architecture and basic features. Section 3 reviews the situation of software for Monte Carlo particle transport in 1994 and today, followed by an overview of discoveries and scientific advancements enabled by Geant4 in Section 4. A discussion of key design aspects is elaborated in Section 5, followed by some concluding remarks and considerations on future perspectives.

2. The Geant4 Simulation Toolkit

2.1. Geant4 Development

Geant4 was developed by the RD44 project [6–9]. Despite the similar name, it represented a radical shift with respect to the GEANT code described in Section 3.1. RD44 gathered an international team of physicists, computer scientists and engineers affiliated with many academic and research institutes worldwide. It took part in the CERN (Conseil Européen pour la Recherche Nucléaire) research and development programme for the experiments [10] at the Large Hadron Collider (LHC) [11], which were expected to become operational in the first decade of the 21st century.

Early considerations about developing an object-oriented Monte Carlo system for particle transport date back to 1993 [12, 13]. They evolved into the formal proposal [14] of Geant4

*Corresponding author, daniele.dagostino@unige.it

¹Retired.

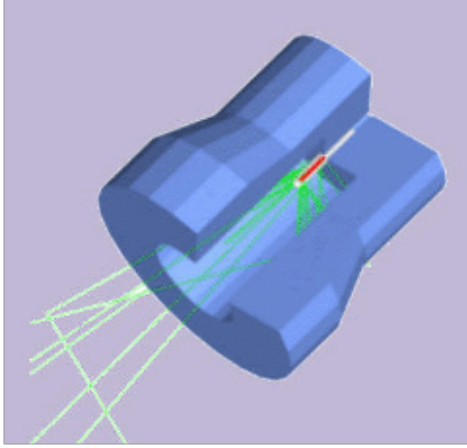


Figure 1: Visualization of a Geant4-based simulation of a radioactive source and its enclosure for application in oncological radiation therapy: the geometrical model reproduces the container of the radioactive source (in red) and the applicator (in blue) used in clinical practice; primary and secondary particles originating from the radioactive source are shown in green.

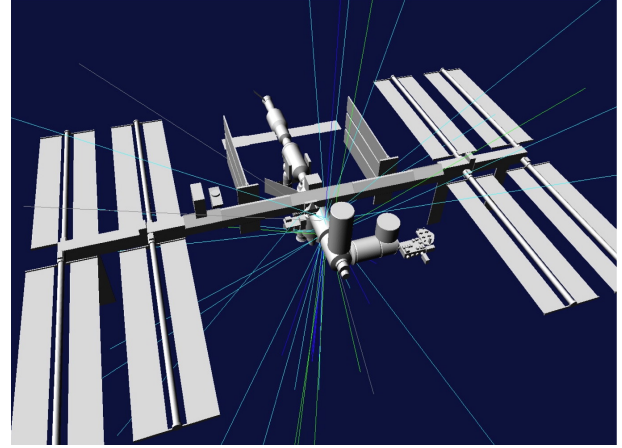


Figure 2: The International Space Station modelled with Geant4.

development, which was approved by the CERN Detector Research and Development Committee (DRDC) as the RD44 project in November 1994. Geant4 was first released on 15 December 1998. The RD44 members are listed in Appendix A.

At the end of the RD44 research and development phase, the maintenance of the Geant4 toolkit was formally taken over by an international team known as the Geant4 Collaboration, which is responsible for releasing new versions of the code and for providing user support.

2.2. Basic Features of Geant4

Geant4 is an object-oriented software toolkit for the simulation of the passage of particles through matter. It tracks particles and models the processes through which they interact with the environment they traverse. Geant4 source code and the associated user documentation can be freely downloaded [15].

Simulation plays a fundamental role in high energy physics experiments – the scientific domain that motivated the development of Geant4. It permeates the whole experimental life-cycle: from the conceptual design of experiments and the optimization of the characteristics of the particle detectors they encompass, to in-depth understanding of their operation, down to the evaluation of various physics and technological factors that contribute to determine the scientific results of an experiment. It is also an essential basis for the development and the refinement of software for data reconstruction using signals recorded by particle detectors, and for data analysis. Similar functions are also common to other experimental scenarios where precise account of the effects of particle interactions with matter is needed, such as space science missions and astrophysics, nuclear power plants, radiation therapy, radiation protection, etc.

Geant4 includes tools for all the functionality typically needed for the simulation of these experimental scenarios: modeling the geometry and materials of the experimental setup, retrieving the properties of elementary and composite particles, modeling the processes particles undergo when interacting with

matter, managing the passage of particles in the experimental setup (articulated over steps, tracks and events) and recording its effects, controlling the execution of the simulation, visualizing the experimental setup and particle trajectories, and providing user interface to the simulation. Additionally, the Geant4 toolkit includes a set of auxiliary tools supporting the core functionality and a rich collection of application examples. Further details can be found in the main Geant4 reference paper [1].

The simulation scenarios illustrated in Figures 1 and 2, pertaining to utterly different application fields and characterized by largely different scales, are suggestive of the versatility of Geant4. Figure 1 reproduces the model of an ^{192}Ir radioactive source used in oncological radiation therapy [16]. The size of brachytherapy applicators, such as the one depicted in the figure, is of the order of a few centimeters. Figure 2 shows the Geant4-based model of the International Space Station [17] exposed to the space radiation environment.

2.3. The Architecture of Geant4

Geant4 is a toolkit: a set of consistent software tools, out of which the user picks those deemed relevant to the experimental problem to be investigated. As a toolkit, Geant4 cannot be “run” by a user: the user must develop an application, specific to the experimental scenario one intends to simulate, which uses the “tools” available in the toolkit. This is a distinctive characteristic of Geant4, which distinguishes it from other Monte Carlo particle transport codes, such as those briefly described in Section 3.

The foundation of Geant4 lies on a rigorous problem domain analysis and related object-oriented design, conceived and progressively refined during the course of the RD44 project, which identified well-defined interfaces and relations between components, making the toolkit easily and consistently extensible. The Geant4 architecture resulting from this process is illustrated in the UML (Unified Modeling Language) package diagram of Figure 3.

Packages at the bottom of the diagram in Figure 3 provide fundamental services to the whole toolkit: *global* deals with basic features (the system of units, physical constants, math-

ematical methods and random numbers); *material* and *geometry* deal with modeling the experimental setup; *particle* encodes particle properties [18]; *graphic_reps* and *intercoms* enclose basic means for graphics and interactions with Geant4 kernel. Packages above them deal with the core of particle transport: *track* hosts the key players of transport – classes responsible for tracks and steps; *processes* deals with particle interactions in the course of transport; *digits_hits* deals with the generation of the responses to physics processes in the experimental setup; *tracking* manages the evolution of particle transport and of its effects in sensitive volumes of the experimental layout. A notable feature of Geant4 architecture is that tracking deals with all processes blindly, i.e. through a single abstract base class: this distinctive feature is the key to the extensibility of Geant4 physics capabilities. The *run* and *event* packages deal with the control of the simulation: in the context of Geant4, an “event” is the minimal unit of simulation, related to the evolution from the creation of primary particles fed into the simulation to the resulting observables in the experimental setup; a “run” manages collections of events characterized by a common experimental scenario. The *interfaces*, *visualisation* and *persistency* packages depend on previously mentioned packages and let the user connect to external facilities through abstract interfaces (i.e. without any external dependencies) to steer the simulation, to produce visual representations and to store persistent products, respectively. A detailed description of Geant4 architecture can be found in the main associated reference [1].

It is worthwhile to note that the architecture depicted in Figure 3 has remained unchanged through the 25 years’ lifetime of Geant4, while the source code evolved from about 283000 lines (excluding comments) in the first version released in December 1998 to more than 872000 lines of the most recent version, 11.2, released in December 2023. The resilience of Geant4 architecture to the extensive evolution of the software and of its applications is a demonstration of the depth of the problem domain analysis and the vision that characterized the RD44 project.

The UML class diagram in Figure 4 illustrates the conceptual organization of a Geant4-based user application. The user instantiates *G4RunManager*, a Geant4 kernel class responsible for orchestrating particle transport in the user-defined experimental scenario, and interacts with the Geant4 kernel in the course of the simulation through a set of initialization and action classes, derived from base classes present in Geant4 kernel. These classes, shown in yellow in Figure 4, allow the user to customize the simulation. They are responsible for the creation of the primary particles to be fed into the simulation, for modeling the experimental setup, for selecting the physics processes and models relevant to the experimental problem to be investigated, and for the interaction with the transport kernel at various stages (run, event, tracking, stepping etc.). An overview of the workflow of using Geant4 in a simple simulation can be found in Geant4 user documentation [19].

While the class diagram in Figure 4 reflects the conceptual configuration of any Geant4-based simulation, the simulation of large-scale experiments using Geant4 is articulated through complex software designs and implementations, such as, for instance, those described in [20–22].

The most critical feature of the simulation of an experimental scenario is the selection of the relevant physics processes, cross sections and final state generation models among the many options available in the Geant4 toolkit. This operation is supported by validation tests of Geant4 physics modeling elements (e.g. [23–26]), complemented by experiment-specific comparisons of the simulation of complex observables (e.g. [27–29]) to corresponding experimental measurements. The validation process allows users to optimize their simulation configuration and to evaluate its contribution to the errors associated with their experimental measurements [30].

2.4. Computational Performance

The computational performance of a Geant4-based simulation intertwines the intrinsic performance of Geant4 elements, the way they are used, and the performance of the user application. Therefore, the performance of a Geant4-based simulation can only be quantified over the specific configuration defined in the application, together with possible inefficiencies in the application code [31].

An exhaustive discussion of Geant4 computational performance exceeds the scope of this paper. In this brief overview, we highlight some features that have played a significant role in the production of scientific results in computationally-intensive simulation applications.

Computational performance has been a concern since the early days of Geant4 development. It was addressed in the RD44 project through a combination of conceptual innovations in the software design and in the implemented algorithms, along with attention to the quality of the software through peer reviews and frequent benchmarks to monitor and optimize the performance of the code.

A common prejudice in the 1990s was the unsuitability of C++ as a programming language for computationally-intensive scientific use. Early benchmarks [7] demonstrated that, thanks to well designed and carefully implemented software, Geant4 achieved much better computational performance than GEANT 3.21, which had been purposely optimized for these assessments, in simulation scenarios specifically devised for performance evaluations.

A major innovation in terms of computational performance was the introduction of the concept of “smart voxels” in Geant4 geometry [32], which significantly improves the performance of tracking particles in the experimental setup, i.e. a most critical task in the simulation of any experimental scenario. Geant4 “smart voxels” extend and enhance the established concept that a hierarchically structured geometry contributes to computational performance of tracking time through the reduction of candidate volumes for intersections. A relevant feature of their implementation is the low computational and memory cost. The optimization realized by this algorithm even reduces the need for revising poorly structured geometries coded by inexperienced users in their applications. Further actions to optimize the performance of tracking, both in Geant4 software design and implementation, are documented in [8].

Another innovative algorithm [33] exploits Geant4’s unique method of dealing with thresholds for secondary particle pro-

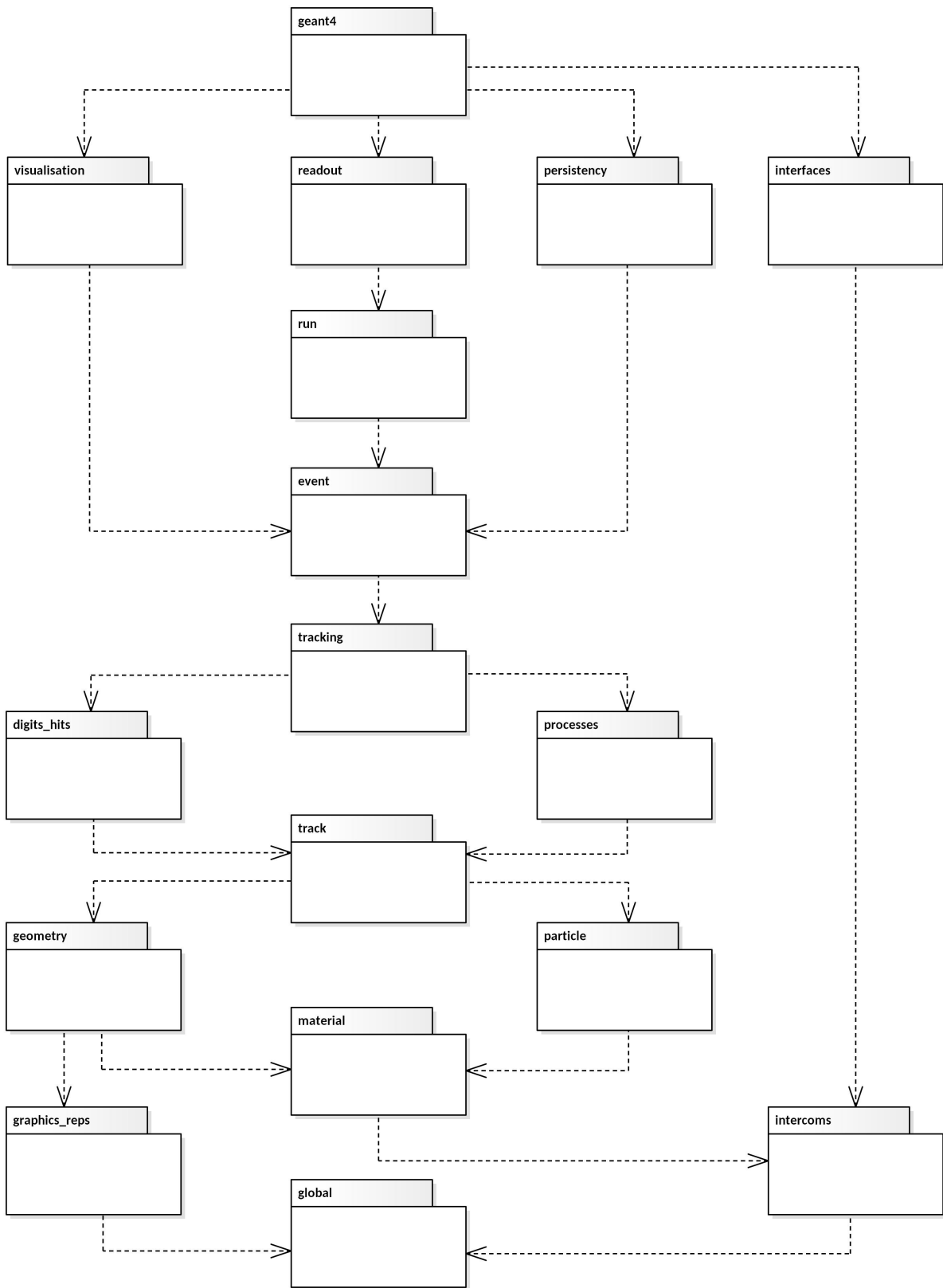


Figure 3: UML package diagram of Geant4, showing the top level packages. Further details and UML diagrams of Geant4 software design can be found in [1].

duction in terms of particle range, rather than on tracking cuts or energy cuts as in other Monte Carlo transport codes. The adoption of secondary particle production in terms of range thresholds simultaneously addresses computational performance and physical accuracy in the occurrence of electromagnetic processes (ionisation and Bremsstrahlung) affected by infrared divergence. It lets processes produce secondary electrons (δ -rays) that would reach geometrical boundaries, thus having a chance to produce observable effects, while it avoids the waste of computational resources for producing and tracking low energy secondary electrons that would not escape from the current volume by locally depositing their energy. As shown in [33], it significantly optimizes the tracking performance for ionizing particles without sacrificing physics accuracy. Further details about performance optimization resting on Geant4 design and algorithms can be found in [7], [8] and [1].

A key factor improving the performance of Geant4 is represented by the adoption of the multithreading paradigm, introduced in version 10 in 2013 [3, 34, 35] in response to the emergence of multi-core and many-core processors [36]. The foundation of this evolution relies on the intrinsic independence of events in Geant4, embodied by the event management originally designed in RD44, which made Geant4 naturally parallelizable. Each thread is responsible for simulating one or more events, thus implementing event-level parallelism; memory savings are obtained by sharing data that remain constant throughout the simulation, such as the geometry model and data used by physics processes.

This solution addresses current experimental requirements; further investigations are in progress in view of the evolution of the requirements of the experiments at the High Luminosity LHC [37], whose operation is currently foreseen in the years 2030-2041, and of the evolution of parallel architectures in the hardware industry. Research on this computational topic involves both experimental teams and members of the Geant4 collaboration, and concerns porting the code to GPU (Graphics Processing Unit) devices [38] as well as the investigation of other candidate solutions.

3. Related Works

3.1. GEANT

Geant4 superseded the GEANT [39, 40] simulation tool previously produced and distributed by CERN.

The GEANT (GEometry ANd Tracking) program was developed as a detector description and simulation tool for particle physics experiments. It was written in Fortran; its development represented at least 50 man-years' work, spread over more than 15 years. The early developments of GEANT did not materialize into proper releases of the code; the first practically usable release was GEANT version 3 in 1984, which evolved through a series of minor versions. The last version, GEANT 3.21, consisting of approximately 63000 lines of code, was released in early 1994; it was maintained by CERN without any further development until 2003.

The main functionality of GEANT consisted of tracking particles through a geometrical data structure. While its geometry and tracking capabilities were refined, GEANT was limited in modeling physics processes. It included functionality to handle basic electromagnetic interactions of particles with matter, but it relied on external packages (GEISHA [41], FLUKA [42] and CALOR [43]) for the simulation of hadronic interactions. The dependency on critical physics code, owned and controlled by external sources, de facto prevented the improvement and the extension of GEANT capabilities in the hadronic physics domain as needed by the evolving requirements of the experiments at CERN and elsewhere. The electromagnetic physics of GEANT lacked adequate modeling capabilities for precision quantification of the effects of particle interactions, especially at very low (< 10 keV) and very high ($\gtrsim 100$ GeV) energies, which are relevant to application fields such as astroparticle physics, medical physics and space science.

A serious drawback of procedural programming in GEANT (common to other simulation codes in Fortran) was the difficulty in extending its functionality in response to requirements that commonly arise in physics research: for instance, nearly 60 subroutines had to be modified, when one wished to implement an additional geometrical shape needed to model an experimental setup. One had to face a similar complication when introducing a new particle type to be tracked.

The success of GEANT in experimental particle physics was largely due to allowing users to plug in routines for handling experiment-dependent code, such as the geometrical description and the digitisation of the signal of detectors, into an infrastructure of experiment-independent code. Nevertheless, the functionality of GEANT was inadequate for the long-term research programs of the experiments in the TeV scale that were being designed in the 1990's and expected to be operational after 2000. The use of GEANT in research areas other than particle physics, such as space science [44] and medical physics [45], was marginal in the mid 1990's.

3.2. Overview of Monte Carlo Particle Transport Codes

Many software systems have been developed for the simulation of particle interactions with matter since the 1940's, when the Monte Carlo method was devised and first applied to physics calculations on early computers [46–48].

Several Monte Carlo particle transport codes are currently utilized in particle, astroparticle, nuclear and medical physics, in space science and related fields along with Geant4. Well-known codes in these domains are EGS5 [49], EGSnrc [50], FLUKA [51], ITS [52], MARS [53], MCNP 6 [54], OpenMC [55], PENELOPE [56], PHITS [57], Serpent [58] and TRIPOLI-4[®] [59]. Some of them have a fairly wide scope of applicability (e.g., MCNP), while others are restricted to specific physics scenarios (e.g. handling only electron and photon interactions) or are targeted to specific experimental application areas (e.g. simulations related to nuclear reactors). Some have been well established in the field for decades (e.g. MCNP, ITS and EGS), while others are relative newcomers (e.g. PHITS, Serpent and OpenMC). Most of them are still written in Fortran; some in-

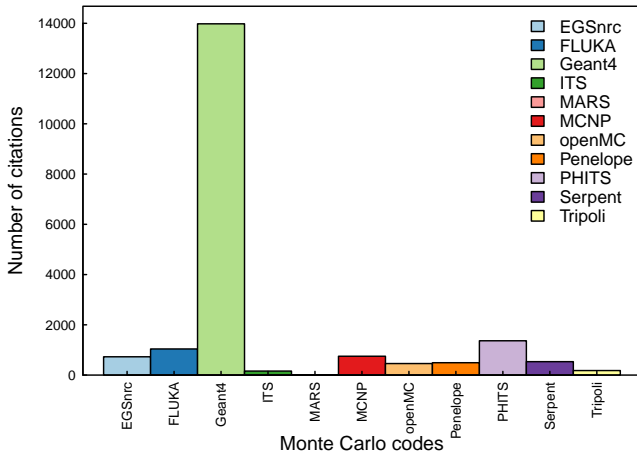


Figure 5: Citations of Monte Carlo codes commonly used in particle, astroparticle, nuclear and medical physics, in space science and related research areas, collected over the years 2003-2023.

clude recently developed parts in C++ along with long-standing Fortran code.

A detailed description of the features of these codes and a discussion of their relative merits is well beyond the scope of this paper; nevertheless, some considerations are helpful to best appraise the role played by Geant4 in enabling the production of scientific results.

Geant4 stands out among Monte Carlo particle transport codes with respect to the number of citations received by the associated reference papers, as is shown in Figure 5. The citation data used in the plot derive from the Web of Science™ [60] and are limited to publications in scholarly journals appearing between 2003 and 2023, inclusive. It should be noted that only a few of the associated references were published in 2003 or earlier; more recently developed codes have necessarily accumulated citations over a reduced portion of the time scale of the plot, nevertheless, the variable extent of collection of citations does not substantially affect the qualitative appraisal of Figure 5.

It is also worthwhile to note that one of the previously mentioned Monte Carlo codes, EGS5, does not appear in the plot due to lacking a dedicated journal publication we could use to extract scientometric data (note that [49] is not a peer-reviewed document). Indeed, user documentation manuals have been for a long time the only writings associated with Monte Carlo transport codes; even codes with a long historical background began publishing dedicated reference articles only relatively recently. This habit reflects the unfounded perception of Monte Carlo transport codes, and of scientific software in general, as mere service tools devoid of scientific relevance in some physics and engineering environments, which was quantitatively assessed in [61]. This attitude is responsible for the frequent omission of proper citation of the existing reference papers of Monte Carlo codes, including Geant4, which was highlighted in [62].

4. The Impact of Geant4 in the Scientific Community

The Geant4 main reference paper has collected more than 16000 citations by the end of 2023 in the Web of Science™, here considered since 1990. It is the most cited publication in the categories of Particle and Fields Physics, Nuclear Physics, Nuclear Science and Technology, Instruments and Instrumentation, and Astronomy and Astrophysics. These categories collectively include more than 2 million papers published in scholarly journals between 1990 and 2023. These data concisely assess the impact of Geant4 on the production of scientific results.

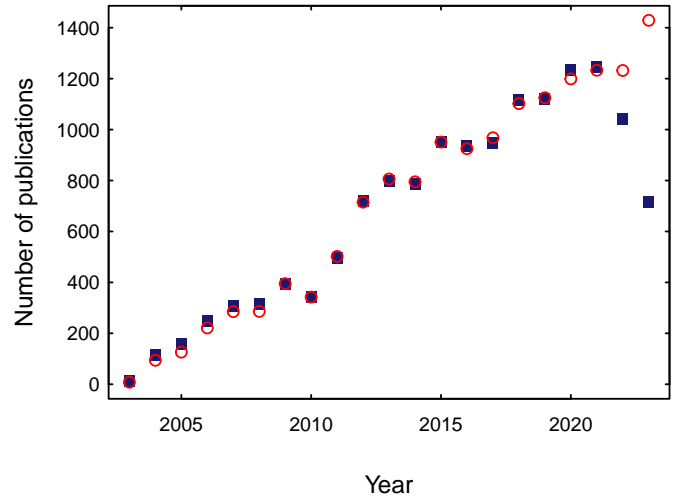


Figure 6: Number of scientific publications citing Geant4 main reference [1] as a function of year: data retrieved from the Web of Science (blue squares) and from Scopus (red circles).

Figure 6 shows the time profile of the citations of Geant4 main reference [1]; it reports data retrieved from the Web of Science™ and from Scopus® [63], concerning journal publications. The two data sets look generally consistent, but some discrepancies are qualitatively visible in the number of citations of the last two years. This apparent anomaly could be related to ongoing updates and corrections of the database underlying the Web of Science; nevertheless, being limited to a small fraction of the data, it does not substantially affect the scientometric results reported in this paper. Mann-Kendall [64, 65] trend tests performed over both sets of citation data, including the whole range of years from 2003 to 2023, reject the null hypothesis of no trend in the data distributions with 0.01 significance in favour of the alternative hypothesis of increasing trend, thus supporting the irrelevance of the two last points in determining the general trend of the data.

Although originally motivated by the requirements of high energy physics experiments, Geant4 encompasses functionality relevant to other research domains. The literature documenting the use of Geant4 is characterized by wide and growing multidisciplinarity: one can observe it in Figure 7, which shows the number of research areas (as defined in the Web of Science) represented in the papers that cite Geant4 main reference [1], as reported by the Web of Science. The increasing multidisciplinarity in the scientific results enabled by Geant4 is ob-

jectively confirmed by statistical inference: the Mann-Kendall test [64, 65] rejects the null hypothesis of no trend in the data distribution of Figure 7 with 0.01 significance in favour of the alternative hypothesis of increasing trend.

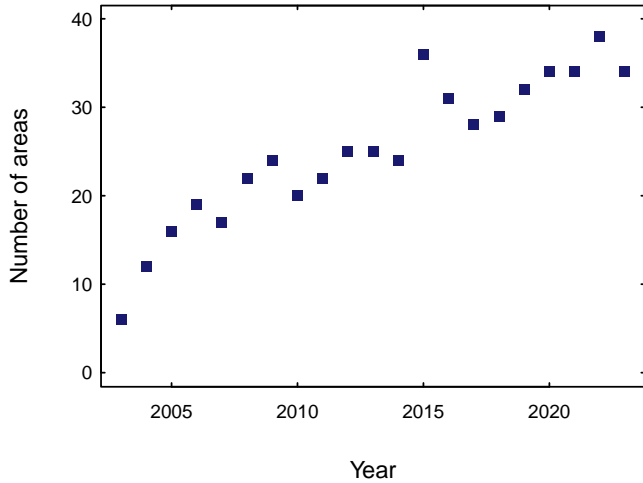


Figure 7: Research areas of the publications citing Geant4 main reference [1] as a function of year.

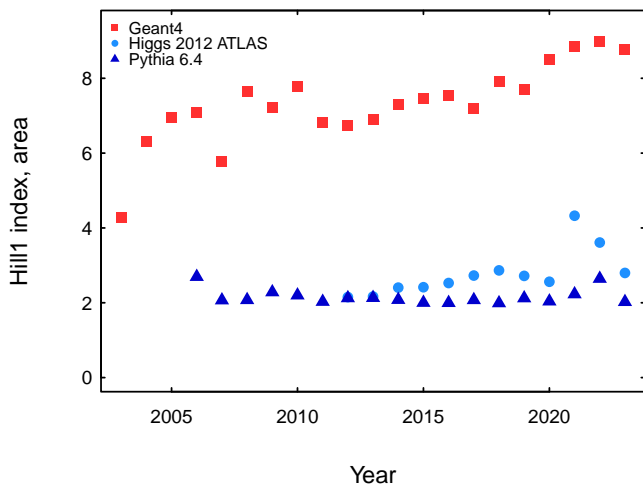


Figure 8: Diversity, as a function of year, of the research areas of origin of the citations of Geant4 main reference [1] (red squares) and of representative high energy physics publications: the report of the discovery of the Higgs boson [4, 5], related to the 2013 Nobel Prize, and the reference paper of the PYTHIA Monte Carlo event generator [66] (blue circles and triangles, respectively). Since the two papers [4, 5] were published simultaneously by the ATLAS and the CMS experiments and are usually jointly cited, the plot only displays the diversity associated with [4] for better clarity.

The multidisciplinary character of the research publications that use Geant4 is further corroborated by the analysis of their diversity. Biodiversity is a concept pertinent to quantitative ecology, where it measures the richness and the complexity of a community, taking into account the number of species it hosts and their abundance. Its mathematical formulations [67] can be applied to the analysis of scholarly publications.

Figure 8 reports the time profile of a well established diversity measure, calculated using scientometric data retrieved

from the Web of Science – the Hill index of order 1 [68], which is related to the definition of Shannon entropy [69] in information theory. The plot shows the diversity of research areas of the citations of Geant4 main reference [1], measured each year over the papers published in that year, and of two significantly representative publications originating from the same domain as Geant4, high energy physics: the observation of the Higgs boson at the LHC, related to the 2013 Nobel Prize in Physics [4, 5], and the reference paper of the PYTHIA [66] Monte Carlo event generator, a highly cited software system used in particle physics. It is evident in Figure 8 that the scientific production enabled by Geant4 exhibits much larger diversity than either of those two papers.

It is practically impossible to document a complete assessment of the scientific research that Geant4 has enabled and of the results that it has contributed to achieve over the past 25 years since its first release. We just single out a few remarkable examples that highlight the multidisciplinary usage of Geant4, in addition to the previously mentioned use of Geant4 in relation to the first observation of the Higgs boson by the ATLAS and CMS experiments [4, 5].

Geant4 played a crucial role in the events that affected the operation of two similar space missions for X-ray astronomy, Chandra and XMM, launched by NASA and ESA (European Space Agency), respectively, in 1999, shortly after the first release of Geant4. Chandra experienced unexpected degradation of the majority of the CCDs (Charge-Coupled Devices) in the ACIS (Advanced CCD Imaging Spectrometer) instrument on board shortly after the launch, which affected the scientific capabilities of the mission. The Geant4-based simulation of XMM [70] prior to its launch identified the cause of the deterioration of Chandra’s detection capabilities, due to low energy (~100 keV) protons reaching the focal plane after scattering through the mirror shells in the experimental setup. This result allowed ESA to take proper countermeasures prior to the launch to avoid similar damage to XMM, which preserved as-designed detection capabilities during its operation in orbit.

Geant4 has been instrumental in enabling a major archeological discovery in Khufu’s (Cheops) pyramid [71] on the Giza plateau in Egypt by means of the muon tomography technique. A large void above the Grand Gallery of the Pyramid has been identified by comparing the expected muon flux, determined by a Geant4-based simulation, and experimental measurements.

Geant4 is widely used in medicine for radiation therapy, radiology, nuclear medicine and radiation protection research; articulated application tools have been developed to facilitate its use for medical investigations. One of them, GATE (Geant4 Application for Tomographic Emission) has become a de facto standard for medical imaging simulations; its reference paper [72] has collected more than 1600 citations in scholarly publications, which demonstrate the extensive contribution of Geant4 to produce research results in this field.

Besides academic research, Geant4 has enabled many applications of industrial relevance. As an example, more than 200 patents related to Geant4 have been issued by the United States Patent and Trademark Office (USPTO) between 2002 and 2023, and more than 600 by the European Patent Office; their distri-

butions are illustrated in Figures 9 and 10. The visible growing trend in the number of Geant4-based patents issued each year is confirmed by the result of the Mann-Kendall test [64, 65], which rejects the null hypothesis of no trend in both data distribution with 0.01 significance, in favour of the alternative hypothesis of increasing trend.

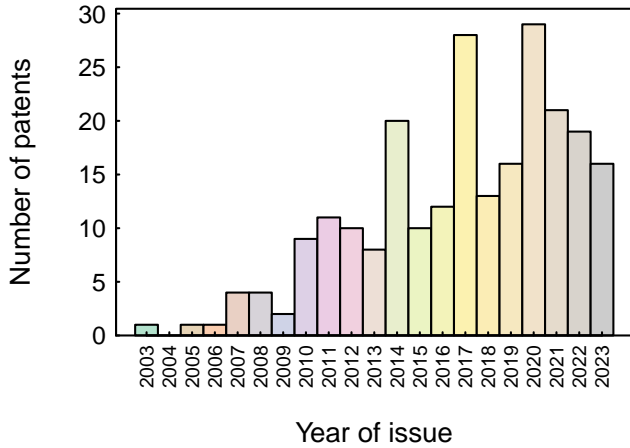


Figure 9: Patents associated with Geant4 issued by the United States Patent and Trademark Office (USPTO).

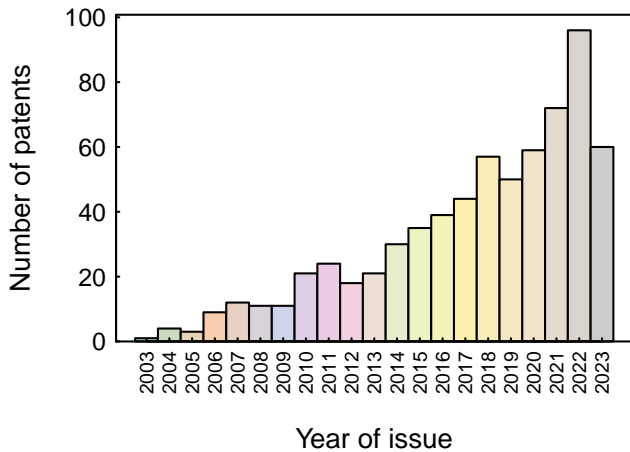


Figure 10: Patents associated with Geant4 issued by the European Patent Office.

5. Software Engineering Foundations

The success of Geant4 at enabling scientific and industrial research results is rooted in its software engineering foundations set by the RD44 project.

RD44 exploited the most advanced software engineering techniques available at the time of its activity (1994-1998) to accomplish a distributed software design and development. It introduced significant innovations in the development of Geant4 with respect to common practice in the computational environment of high energy physics and related physics research areas, and in the domain of Monte Carlo simulation for particle transport. The role of software engineering as a key strategy to pro-

duce a high-quality scientific software system and to release it in time represented a major novelty in these fields.

5.1. Open Source Code

Geant4 openness and transparency have been major concerns of the RD44 project since its initial conception. Open access to the source code is a necessity for physics software. Since the simulation software affects the outcome of the experiments that use it, ability to examine, understand and appraise the source code is a critical requirement for the validation of the experimental results and, ultimately, for their reproducibility, which is an essential feature of the scientific method.

Geant4 is freely available as open source software. It is worthwhile to note that open access to the source code is not general practice for Monte Carlo particle transport systems: for instance, the standalone FLUKA [51] code is not publicly distributed and the MCNP [54] code is subject to the export control laws of the United States restricting the distribution of the source code.

Apart from its essential epistemological role in the production of scientific results, the open source character of Geant4 code plays an important role in allowing scientists to extend the functionality of the toolkit. Several users' extensions and improvements have been incorporated into the Geant4 toolkit over the years, to the benefit of the whole user community.

5.2. Turnarounds in Particle Physics Computing

At the start of RD44, two paradigms had dominated the computational environment of particle physics since the 1960's: the Fortran programming language and the use of mainframes.

Procedural programming and Fortran (with the MORTRAN variant, a Fortran extension used by EGS) were the rule in particle physics and in Monte Carlo particle transport in general at the time when RD44 proposed the development of Geant4 in 1994. The CERN Program Library (CERNLIB) [73], which included the GEANT 3 code, was for decades one of the largest and most advanced collections of scientific software. As documented in [74] and [75], between 1979 and the end of its support in 2003, 80% of its programs were written in Fortran and the remainder in assembler code or C, usually with a Fortran version also available.

Geant4 represented the first attempt to redesign a major package of CERN software for an object-oriented environment. The adoption of the object-oriented paradigm and of C++ as programming language for Geant4 represented a breakthrough in the particle physics environment and in Monte Carlo particle transport.

The choice of the object-oriented technology broadened the horizon and generalized the potential for scientific research with respect to any previous software development project in the high energy physics environment. One could envisage dealing transparently with any experimental scenario, regardless of whether it was a particle detector or the human body, or propagating particles through any field - magnetic, electric or gravitational. The unbounded versatility associated with the object-oriented technology introduced an additional requirement of

generalization and flexibility into Geant4 software: the simulated physics processes must deal with an unprecedented energy range, from approximately 100 eV to the scale of PeV, i.e. orders of magnitude above and below the energies addressed by GEANT 3 and other Monte Carlo particle transport codes listed in Section 3.2.

This adoption of the object-oriented paradigm, carried out through well defined interfaces between components and coupled with the open source character of the code, has allowed scientists to extend the functionality of Geant4 in response to a wide variety of experimental requirements. Geant4 software design intrinsically supports multidisciplinary through its openness to extension and customization and is the key factor behind the wide variety of research areas represented in the scientific publications using Geant4, discussed in Section 4.

The choice of C++ as the programming language for the implementation of Geant4 was motivated by objective considerations: its characteristic of being a de facto standard, its use in industry, the availability of relevant development tools and the expectation of a long lifetime. These characteristics have contributed to the longevity of Geant4, avoiding the risk of rapid obsolescence of the code and of its computational environment.

The use of mainframes meant that computing was conceived as a service provided to a user sitting at a terminal and holding an account granted by a computing centre that had full control over the programs available to the users. Monte Carlo simulation fell into this scheme. The availability of personal computers, which characterized the evolution of high energy physics computing in the 1990s, enabled a scenario where the user became someone who worked and traveled with her/his own computer, with the freedom of using the programs of her/his own choice and the ability to connect with any other computer via the Internet.

RD44 effectively exploited the perspective of moving from computing based on a mainframe architecture to personal computers and to heterogeneous High Performance Computing environments, from the TOP500 systems down to Beowulf clusters, avoiding any technological lock-in as, for example, due to proprietary inter-node communication libraries.

The conception of Geant4 as a toolkit and its well-defined interfaces to external systems for visualization, user interface, persistency etc., which shield users from forced dependencies, grant users the autonomy to shape their simulation environment as they deem appropriate to their experimental scenarios. This resolution has also facilitated Geant4 users to devise high performance simulations based on commodity hardware for computationally intensive experimental scenarios since the earliest Geant4 releases. This approach is especially significant in the case of small research teams and limited resources, which are largely represented among the publications reporting scientific results based on Geant4 [76].

The freedom of choice enabled by these strategic directions taken by RD44, which lets users tailor the computational environment and the behaviour of the software, including the ability to extend its functionality, is at the basis of the outstanding amount and diversity of the research results associated with Geant4, documented in Section 4.

5.3. Distributed Development

The RD44 project introduced a novel approach to the development of a general-purpose physics simulation tool as a geographically distributed project.

Previous simulation systems for particle transport were generally developed by small teams, usually based at a research laboratory or at an academic institute: notable examples are [41–43, 77–80]. The GEANT 3 [40] code – the predecessor of Geant4 at CERN – was the product of a CERN service unit operating in a dedicated computing department, with occasional contributions of a few visiting scientists. High energy physics experiments in laboratories other than CERN commonly used CERN service software, namely the CERN Program Library CERNLIB, which included the GEANT code.

The RD44 project was a large international team of physicists, computer scientists and engineers, based at several laboratories, research institutes and universities worldwide. The distributed development pattern was fundamental to involve scientists with a wide spectrum of skills in all the physical, mathematical and technological aspects of the complex problem domain, which contributed to both the richness of Geant4 functionality and the quality of the toolkit. The distributed character also introduced cooperative management of the project, whose participants originated from different research areas and experiments that shared some common requirements, but differed in relation to others. This trait was the seed of Geant4’s multidisciplinary and significantly impacted the characteristics of the software.

Key features of RD44 distributed software development process are documented in [7–9]. They included configuration management, which dealt with version control and tags, incremental testing, which took into account package dependencies with respect to the architectural design and related to traceability matrices, and 24-hour release cycles.

Distributed development was supported in RD44 by tools that represented the state of the art at that time, such as CVS (Concurrent Version System) for version control and Rational Rose for object-oriented analysis and design, along with tools developed within the RD44 team in response to specific needs, such as unit testing and management of 24-hour release cycles. Their use evolved with time, along with general evolution in the field – e.g., from CVS to SVN (Subversion) [81], then to git [82] – and with the transition from RD44, a research project, to the regime of the Geant4 Collaboration, characterized by maintenance and support service to the user community.

5.4. Software Development Process

The research and development phase of Geant4 took four years (1995–1998), following an iterative approach with progressive refinement of user requirements, design, implementation and tests. This software development strategy was critical to address the tremendous complexity of the problem domain while performing a major transition to computational paradigms that were a novelty in the field of particle physics.

RD44’s explicit adoption of a software development model represented an innovation by itself in the particle physics envi-

ronment. The development process included several new activities – for instance, a 24-hour testing and release cycle that today is common practice, but in the 1990’s it was mostly unknown in physics software and seldom adopted even in professional software development environments.

Embracing an iterative and incremental software development process, based on the Booch methodology [83], was the key to cope successfully with the aggressive development schedule imposed by the external constraints of the LHC experimental program. The RD44 project fulfilled all the milestones set by the CERN Scientific Committees in the course of its lifetime and delivered the first public version of Geant4 on time, with the required functionality.

At the end of RD44, the software development process conformed to the transition from a fiercely innovative research project to the activity oriented to maintenance and user support in the environment of the Geant4 Collaboration. Research on development methodologies is still pursued in some frontier activities, whose innovative character benefits from the refinement of development methods adopted in RD44 and the exploration of new methodologies, with the support of pertinent tools. In this context, [84] reports the use of BPMN (Business Process Model and Notation) [85] and of ArchiMate [86], with focus on identifying the role of these technologies in physics research.

5.5. Usability and sustainability

The adoption of new computing paradigms and the use of an unfamiliar programming language required clever efforts to ensure the usability of Geant4 in experimental physics applications. Several actions, planned in the course of the RD44 project and carried out since the initial Geant4 release, have contributed to Geant4 usability: the inclusion in the toolkit of a wide collection of application examples, encompassing the illustration of various features as well as simulations of realistic experimental scenarios, a series of introductory seminars at laboratories and universities, and several presentations at international scientific conferences and local meetings to inform the diverse user communities about novelties and achievements especially relevant to their field. Today, learning Geant4 is included in the academic programs of physics and engineering degrees at many universities worldwide.

Under the regime of maintenance of the international Geant4 collaboration, the code has been updated to align with the C++11 and C++17 standards, to comply with the evolution of compilers and to exploit the multithreading capabilities available in recent hardware [3]. Thanks to the sound software design established in the RD44 project, the original functionality of Geant4 has been extended in many areas with the contribution of both formal collaboration members and users. Source code and application examples donated by users are maintained by collaboration members to ensure their long term availability when long-term commitment of the original contributors is not possible.

6. Conclusion and Future Perspectives

Geant4 is still actively used 25 years since its initial release. As shown in Section 4, the number of citations of its main reference paper and of patents based on it has been steadily growing.

Based on its usage and citations, Geant4 has been the most impactful Monte Carlo software code in an extended scientific community for 25 years. It has been applied in a wide variety of scientific fields, ranging from high energy physics to nuclear medicine to space science to archaeology. Some key factors have contributed to its longevity and broad applicability: the code has been open source, allowing users to contribute improvements and extensions of functionality; it used an object-oriented software paradigm, which provided a toolkit with large flexibility in applying it to a variety of experimental scenarios; it was written in a modern, widely used, long-lived programming language; the development team was broad-based, both geographically and scientifically. The directions taken by RD44, which today represent good software development practice, represented pioneering principles and cutting-edge technology the 1990s in the field of high energy physics.

Geant4 is expected to remain a reference simulation software into the future, thanks to its widespread use in many application areas, its openness to improvements and extension in response to experimental requirements, and the Geant4 collaboration’s continual commitment to its maintenance. An extensive discussion of Geant4 future perspectives exceeds the scope of this paper; below are a few topics of current interest in the domain of Monte Carlo particle transport, which are likely to be the object of research in the field in the coming years.

The need to increase simulation throughput is common to various application environments, from experiments at high luminosity colliders to personalized medical treatments. Ongoing work to introduce sub-event parallelism [87] and to demonstrate the feasibility and efficiency of adopting the GPU computing paradigm involves revisiting computationally intensive parts of Geant4 code. Increasing heterogeneity in computing architectures, where a single CPU can provide 128 cores (e.g. AMD EPYC Bergamo) or more by merging CPU and GPU cores (e.g. AMD Instinct MI300A), would demand further investment to keep up with the evolution of computing hardware.

State-of-the-art computational performance is needed not only by large scale Geant4-based simulations, but also for Uncertainty Quantification, an emerging discipline in predictive computational science [88]. In the domain of particle transport, it represents the ability to objectively quantify the degree of reliability of the outcome of a simulation on the basis of the uncertainties in the simulation model [89] and involves developments for the propagation of errors from the data used by the simulation to its results. This capability is especially relevant to critical applications, e.g. in medicine and radiation protection, and to scenarios where either cost or practical constraints prevent assessing the reliability of complex simulated observables by means of direct experimental measurements. Multidisciplinary research, involving mathematical, statistical, computational and epistemological aspects, is required to this end.

Uncertainty Quantification is closely related to the valida-

tion of Geant4 physics “ingredients”: atomic and nuclear parameters, interaction cross sections, modelling methods and algorithms, etc. Currently, only a small fraction of their validation tests use rigorous statistical methods, able to produce objective, quantitative results. Experimental measurements needed for validation are scarce or insufficiently precise in some areas; the new paradigm of computational simulation promoted in [90], which argued the need of funding experiments explicitly conducted for code validation, is far from established. Progress in this domain would be beneficial.

Two key factors characterized the creation of Geant4: the vision that shaped the RD44 project as original, innovative scientific research rather than as a mere computational service, and the talent to make the most of the skills and diversity of all participants towards a shared goal. They were crucial to cope successfully with the technical and environmental challenges outlined in Section 5. They would still be valuable guidelines for the future of Geant4.

Acknowledgements

The authors acknowledge many valuable discussions with RD44 members and Geant4 users. The CERN Library has been especially helpful to retrieve hard-to-find literature.

Appendix A. RD44 Project

The link to the list of RD44 members in the final project report [9] is broken; the list is below to properly credit the RD44 members for their contribution to the development of Geant4.

The members of the RD44 project were: J. Allison (Manchester Univ.), K. Amako (KEK), N. Ameline (JINR), J. Apostolakis (CERN), C. Arnault (LAL, Orsay), P. Arce (Univ. Santander), M. Asai (Hiroshima Inst. of Tech.), D. Axen (UBC), G. Ballocci (INFN Padova), G. Barrand (LAL, Orsay), A. Boehnlein (FNAL), J. Boudreau (Pittsburgh Univ.), B. Caron (Alberta Univ.), J. Chuma (TRIUMF), G. Cosmo (SLAC), C. Dallapiccola (Univ. Maryland), R. Davis (Alberta Univ.), A. Dell’Acqua (CERN), A. Faust (Alberta Univ.), L. Felawka (TRIUMF), A. Feliciello (INFN Torino), H. Fesefeldt (RWTH Aachen), G. Folger (CERN), A. Forti (Milan Univ.), C. Fukunaga (Tokyo Metropolitan Univ.), S. Giani (CERN), A. Givernaud (Saclay), R. Gokieli (INS Warsaw), I. Gonzalez Caballero (CERN), G. Greeniaus (Alberta Univ.), V. Grichine (Lebedev Inst. Moscow), P. Gumplinger (TRIUMF), R. Hamatsu (Tokyo Metropolitan Univ.), S. Hayashi (Hiroshima Inst. of Tech.) M. Heikkinen (Helsinki Inst. of Physics), N. Hoimyr (CERN), P. Jacobs (LBL), F. Jones (TRIUMF), J. Kallenbach (FNAL), J. Kanzaki (KEK), N. Katayama (KEK), P. Kayal (Alberta Univ.), P. Kent (Bath Univ.), A. Kimura (Niigata Univ.), T. Kodama (Naruto Univ. of Education), M. Komogorov (JINR), R. Kokoulin (MEPhI, Moscow), C. Kost (TRIUMF), S. Kunori (FNAL), H. Kurashige (Kyoto Univ.), V. Krylov (JINR), M. Laidlaw (TRIUMF), E. Lamanna (INFN Roma), W. Langeveld (SLAC), V. Lara (Valencia Univ.), F. Lei (Univ. of Southampton), W. Lockman (UCSC), S. Magni (INFN Milano), M. Maire (LAPP),

N. Mokhov (FNAL), A. Mokhtarani (LBL), P. Mora de Freitas (PNHE), Y. Morita (KEK), K. Murakami (Kyoto Univ.), M. Nagamatsu (Naruto Univ. of Education), Y. Nakagawa (International Christian Univ.), I. Nakano (Okayama Univ.), M. Nakao (Okayama Univ.), P. Nieminen (ESA ESTEC), T. Obana (Naruto Univ. of Education), A. Olin (TRIUMF), K. Ohtubo (Fukui Univ.), A. Osborne (CERN), G. Parrou (Orsay), A. Pavliouk (JINR), M. G. Pia (INFN Genova), J. Pinfold (Alberta Univ.), S. Piperov (Humboldt Univ. Berlin), S. Prior (De Montfort Univ.), P. Routenburg (Alberta Univ.), A. Rybin (IHEP Protvino), S. Sadilov (IHEP Protvino), F. Safai Tehrani (INFN Roma), I. Sakai (Tokyo Metropolitan Univ.) H. Sakamoto (Kyoto Univ.), T. Sasaki (KEK), X. Shi (LLNL), L. Silvestris (INFN Bari), V. Sirotenko (North Illinois Univ.), Y. Smirnov (JINR), M. Takahata (Niigata Univ.), N. Takashimizu (KEK), N. Tamura (Niigata Univ.), S. Tanaka (Fukui Univ.), E. Tcherniaev (IHEP Serpukhov), C. Thiebaut (PNHE), P. Truscott (DERA), T. Ullrich (Yale Univ.), T. Umeda (Okayama Univ.) H. Uno (Naruto Univ. of Education), L. Urban (KFKI Budapest), P. Urban (Budapest Tech. Univ.), M. Verderi (PNHE), C. Volcker (München Univ.), A. Walkden (Manchester Univ.), W. Wander (MIT), P. Ward (Univ. Manchester), H. Wellisch (CERN), T. Wenaus (LLNL), D. Williams (U. C. Santa Cruz), D. Wright (TRIUMF), D. Wright (LLNL), H. Yagi (Okayama Univ.), T. Yamagata (International Christian Univ.), T. Yamaguti (Okayama Univ.), Y. Yamashita (Nippon Dental Univ.), Y. Yang (TRIUMF), J. Yarba (FNAL), H. Yoshida (Naruto Univ. of Education), C. Zeitnitz (Mainz Univ.).

References

- [1] S. Agostinelli, et al., Geant4 a simulation toolkit, *Nucl. Instrum. Meth. A* 506 (3) (2003) 250–303.
- [2] J. Allison, et al., Geant4 developments and applications, *IEEE Trans. Nucl. Sci.* 53 (1) (2006) 270–278.
- [3] J. Allison, et al., Recent developments in Geant4, *Nucl. Instrum. Meth. A* 835 (2016) 186–225.
- [4] G. Aad, et al., Observation of a new particle in the search for the Standard Model Higgs boson with the ATLAS detector at the LHC, *Phys. Lett. B* 716 (1) (2012) 1–29.
- [5] S. Chatrchyan, et al., Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC, *Phys. Lett. B* 716 (1) (2012) 30–61.
- [6] S. Giani, et al., RD44 - GEANT 4: an Object-Oriented toolkit for simulation in HEP, <https://greybook.cern.ch/experiment/detail?id=RD44> (1998).
- [7] G. Cosmo, S. Giani, N.-J. e. a. Høimyr, GEANT4: An Object-Oriented Toolkit for Simulation in HEP, *Tech. Rep. CERN-LHCC-95-70*, CERN, Geneva, Switzerland (1995).
- [8] S. Giani, GEANT4: An Object-Oriented Toolkit for Simulation in HEP, *Tech. Rep. CERN/LHCC97-40*, CERN, Geneva, Switzerland (1997).
- [9] S. Giani, GEANT4: An Object-Oriented Toolkit for Simulation in HEP, *Tech. Rep. CERN/LHCC98-44*, CERN, Geneva, Switzerland (1998).
- [10] T. S. Virdee, Detectors at LHC, *Physics Reports* 403-404 (2004) 401–434. doi:<https://doi.org/10.1016/j.physrep.2004.08.026>.
- [11] M. Price, The LHC project, *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment* 478 (1) (2002) 46–61, proceedings of the ninth Int.Conf. on Instrumentation. doi:[https://doi.org/10.1016/S0168-9002\(01\)01717-X](https://doi.org/10.1016/S0168-9002(01)01717-X).
- [12] Y. Takaiwa, et al., Towards Object-Oriented GEANT - ProdiG Project, in: *MC 93 - Proc. Int. Conf. Monte Carlo Simulation in High Energy and Nuclear Physics*, World Scientific, 1994, pp. 339–350.

- [13] S. Giani, Investigation of a class hierarchy for GEANT, Presented at the Mini-workshop on Object-Oriented GEANT, CERN/CN/AS (24-27 Aug. 1993).
- [14] A. Dellacqua, et al., GEANT4: an Object-Oriented toolkit for simulation in HEP, Tech. Rep. CERN/DRDC/P58, CERN, Geneva, Switzerland (1994).
- [15] Geant4, <https://cern.ch/geant4>.
- [16] F. Foppiano, S. Guatelli, J. Moscicki, M. Pia, From DICOM to GRID: a dosimetric system for brachytherapy born from HEP, in: 2003 IEEE Nuclear Science Symposium. Conference Record, Vol. 3, 2003, pp. 1746–1750 Vol.3. doi:10.1109/NSSMIC.2003.1352216.
- [17] T. Ersmark, P. Carlson, E. Daly, C. Fuglesang, I. Gudowska, B. Lund-Jensen, P. Nieminen, M. Pearce, G. Santin, Geant4 Monte Carlo Simulations of the Galactic Cosmic Ray Radiation Environment On-Board the International Space Station/Columbus, IEEE Transactions on Nuclear Science 54 (5) (2007) 1854–1862. doi:10.1109/TNS.2007.906276.
- [18] R. L. Workman, et al., Review of Particle Physics, Progress of Theoretical and Experimental Physics 2022 (8) (2022) 083C01. doi:10.1093/ptep/ptac097.
- [19] Geant4 Book for Application Developers, Release 11.2, Chapter 2, <https://geant4-userdoc.web.cern.ch/UsersGuides/ForApplicationDeveloper/html/index.html>.
- [20] G. Aad, B. Abbott, J. Abdallah, A. Abdelalim, A. Abdesselam, O. Abdinov, B. Abi, M. Abolins, H. Abramowicz, et al., The ATLAS simulation infrastructure, The European Physical Journal C 70 (3) (2010) 823–874.
- [21] S. Banerjee, CMS Simulation Software, Journal of Physics: Conference Series 396 (2) (2012) 022003. doi:10.1088/1742-6596/396/2/022003.
- [22] M. Clemencic, G. Corti, S. Easo, C. R. Jones, S. Miglioranzi, M. Pappagallo, P. Robbe, (on behalf of the LHCb Collaboration), The LHCb Simulation Application, Gauss: Design, Evolution and Experience, Journal of Physics: Conference Series 331 (3) (2011) 032023. doi:10.1088/1742-6596/331/3/032023.
- [23] J. Beringer, G. Folger, F. Gianotti, A. Ribon, J. Wellisch, D. Barberis, M. Cervetto, B. Osculati, Validation of Geant4 hadronic physics, in: 2003 IEEE Nuclear Science Symposium Conference Record, Vol. 1, 2003, pp. 494–498. doi:10.1109/NSSMIC.2003.1352091.
- [24] M. C. Han, H. S. Kim, M. G. Pia, T. Basaglia, M. Batic, G. Hoff, C. H. Kim, P. Saracco, Validation of Cross Sections for Monte Carlo Simulation of the Photoelectric Effect, IEEE Trans. Nucl. Sci. 63 (2) (2016) 1117–1146. doi:10.1109/TNS.2016.2521876.
- [25] T. Basaglia, M. G. Pia, P. Saracco, Evolutions in Photoelectric Cross Section Calculations and Their Validation, IEEE Trans. Nucl. Sci. 67 (3) (2020) 492–501. doi:10.1109/TNS.2020.2971173.
- [26] H. Seo, M. G. Pia, P. Saracco, C. H. Kim, Ionization Cross Sections for Low Energy Electron Transport, IEEE Trans. Nucl. Sci. 58 (6) (2011) 3219–3245. doi:10.1109/TNS.2011.2171992.
- [27] A. Natocchii, S. E. Vahsen, H. Nakayama, T. Ishibashi, S. Terui, Improved simulation of beam backgrounds and collimation at superkekb, Phys. Rev. Accel. Beams 24 (2021) 081001. doi:10.1103/PhysRevAccelBeams.24.081001.
- [28] M. Chefdeville, et al., Analysis of testbeam data of the highly granular RPC-steel CALICE digital hadron calorimeter and validation of Geant4 Monte Carlo models, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment 939 (2019) 89–105. doi:https://doi.org/10.1016/j.nima.2019.05.013.
- [29] V. Morgunov, P. Hybler, M. Zachar, Geant4 validation for x-ray treatment of wooden cultural heritage artefacts, Applied Radiation and Isotopes 169 (2021) 109565. doi:https://doi.org/10.1016/j.apradiso.2020.109565.
- [30] P. Saracco, M. G. Pia, Propagation of input uncertainties in particle transport and the distribution of the sum of n independent stochastic variables a generalization of the irwin-hall distribution, Chinese Journal of Physics 55 (3) (2017) 652–666.
- [31] V. Kourlitis, A. Sukharev, M. A. Schmidt, M. Novak, E. Tcherniaev, G. Amadio, J. D. Chapman, B. Morgan, D. Kim, W. Hopkins, et al., Optimizing the ATLAS Geant4 detector simulation software, Tech. rep., ATL-COM-SOFT-2023-003 (2023).
- [32] P. Kent, Pure tracking and geometry in GEANT4, Tech. rep., CERN, Geneva (1995).
- [33] J. Apostolakis, S. Giani, M. Maire, L. Urban, An algorithm to optimize the tracking of ionizing particles, Tech. rep., CERN, Geneva (1999). URL <https://cds.cern.ch/record/406279>
- [34] X. Dong, G. Cooperman, J. Apostolakis, Multithreaded Geant4: Semi-automatic Transformation into Scalable Thread-Parallel Software, in: Euro-Par 2010 - Parallel Processing, Springer Berlin Heidelberg, Berlin, Heidelberg, 2010, pp. 287–303.
- [35] X. Dong, G. Cooperman, J. Apostolakis, S. Jarp, A. Nowak, M. Asai, D. Brandt, Creating and Improving Multi-Threaded Geant4, Journal of Physics: Conference Series 396 (5) (2012) 052029. doi:10.1088/1742-6596/396/5/052029.
- [36] S. Farrell, A. Dotti, M. Asai, P. Calafiura, R. Monnard, Multi-threaded Geant4 on the Xeon-Phi with complex high-energy physics geometry, in: 2015 IEEE Nuclear Science Symposium and Medical Imaging Conference (NSS/MIC), 2015, pp. 1–4. doi:10.1109/NSSMIC.2015.7581868.
- [37] O. Aberle, et al., High-Luminosity Large Hadron Collider (HL-LHC): Technical design report, CERN Yellow Reports: Monographs, CERN, Geneva, 2020. doi:10.23731/CYRM-2020-0010.
- [38] G. Amadio, J. Apostolakis, P. Buncic, G. Cosmo, D. Dosaru, A. Gheata, S. Hageboeck, J. Hahnfeld, M. Hodgkinson, B. Morgan, et al., Offloading electromagnetic shower transport to GPUs, in: Journal of Physics: Conference Series, Vol. 2438, IOP Publishing, 2023, p. 012055.
- [39] R. Brun, R. Hagelberg, J.-C. Lassalle, M. Hansroul, Simulation program for particle physics experiments, geant: user guide and reference manual, Tech. rep., CM-P00059731 (1978).
- [40] R. Brun, F. Bruyant, F. Carminati, S. Giani, M. Maire, A. McPherson, G. Patrick, L. Urban, GEANT: Detector Description and Simulation Tool, Tech. Rep. Long Writeup W5013, CERN, Geneva, Switzerland (1994).
- [41] H. Fesefeldt, The simulation of hadronic showers: physics and applications, Tech. Rep. PITHA-85-02, RWTH Aachen (1985).
- [42] J. Ranft, The FLUKA and KASPRO hadronic cascade codes, in: Computer Techniques in Radiation Transport and Dosimetry, Springer, 1980, pp. 339–371.
- [43] T. Gabriel, J. Amburgey, B. Bishop, CALOR: a Monte Carlo program package for the design and analysis of calorimeter systems, Tech. rep., Oak Ridge National Lab. (1977).
- [44] G. Malaguti, E. Caroli, A. Dean, G. Di Cocco, F. Lei, A. Spizzichino, B. Swinyard, M. Trifoglio, A Monte-Carlo study of a 3-D position sensitive detector for gamma-ray astronomy, Advances in Space Research 11 (8) (1991) 343–347. doi:https://doi.org/10.1016/0273-1177(91)90186-N.
- [45] C. Michel, A. Bol, T. Spinks, D. Townsend, D. Bailey, S. Grootoink, T. Jones, Assessment of response function in two PET scanners with and without interplane septa, IEEE Transactions on Medical Imaging 10 (3) (1991) 240–248. doi:10.1109/42.97571.
- [46] N. Metropolis, S. Ulam, The Monte Carlo Method, Journal of the American Statistical Association 44 (247) (1949) 335–341. doi:10.1080/01621459.1949.10483310.
- [47] J. von Neumann, Various techniques used in connection with random digits, National Bureau of Standards Applied Mathematics Series 12 (1951) 36–38.
- [48] T. Haigh, M. Priestley, C. Rope, Los Alamos Bets on ENIAC: Nuclear Monte Carlo Simulations, 1947-1948, IEEE Annals of the History of Computing 36 (3) (2014) 42–63. doi:10.1109/MAHC.2014.40.
- [49] H. Hirayama, Y. Namito, A. F. Bielajew, S. J. Wilderman, W. R. Nelson, The EGS5 code system, Tech. Rep. SLAC-R-730, KEK-2005-8, KEK-REPORT-2005-8, SLAC (2005).
- [50] I. Kawrakow, Accurate condensed history Monte Carlo simulation of electron transport. I. EGSnrc, the new EGS4 version, Med. Phys. 27 (3) (2000) 485–498.
- [51] T. Böhlen, et al., The FLUKA code: developments and challenges for high energy and medical applications, Nucl. Data Sheets 120 (2014) 211–214.
- [52] J. A. Halbleib, et al., ITS: the integrated TIGER series of electron/photon transport codes-Version 3.0, IEEE Trans. Nucl. Sci. 39 (4) (1992) 1025–1030.
- [53] N. V. Mokhov, et al., Recent enhancements to the MARS15 code, Radiat. Prot. Dosim. 116 (1-4) (2005) 99–103.
- [54] T. Goorley, et al., Initial MCNP6 release overview, Nucl. Technol. 180 (3) (2012) 298–315.

- [55] P. K. Romano, B. Forget, The OpenMC Monte Carlo particle transport code, *Ann. Nucl. Energy* 51 (2013) 274–281.
- [56] J. Baro, et al., PENELOPE: An algorithm for Monte Carlo simulation of the penetration and energy loss of electrons and positrons in matter, *Nucl. Instrum. Meth. B* 100 (1) (1995) 31–46.
- [57] H. Iwase, et al., Development of general-purpose particle and heavy ion transport Monte Carlo code, *J. Nucl. Sci. Technol.* 39 (11) (2002) 1142–1151.
- [58] J. Leppanen, et al., The Serpent Monte Carlo code: Status, development and applications in 2013, *Ann. Nucl. Energy* 82 (2015) 142–150.
- [59] E. Brun, et al., TRIPOLI-4, CEA, EDF and AREVA reference Monte Carlo code, *Ann. Nucl. Energy* 82 (2015) 151–160.
- [60] Clarivate, The Web of Science™, <http://apps.webofknowledge.com/> (December 2023).
- [61] T. Basaglia, Z. W. Bell, P. V. Dressendorfer, A. Larkin, M. G. Pia, Writing software or writing scientific articles?, *IEEE Transactions on Nuclear Science* 55 (2) (2008) 671–678. doi:10.1109/TNS.2008.919563.
- [62] T. Basaglia, Z. W. Bell, A. Burger, P. V. Dressendorfer, M. G. Pia, Ghost science, in: 2017 IEEE Nucl. Sci. Symp. Medical Imaging Conf., 2017, pp. 1–2.
- [63] Elsevier, Scopus®, <http://www.scopus.com/> (December 2023).
- [64] H. B. Mann, Nonparametric test against trend, *Econometrica* 13 (3) (1945) 245–259.
- [65] M. G. Kendall, Rank Correlation Methods, Griffin, 1948.
- [66] T. Sjostrand, S. Mrenna, P. Skands, PYTHIA 6.4 physics and manual, *Journal of High Energy Physics* 2006 (05) (2006) 026. doi:10.1088/1126-6708/2006/05/026.
- [67] M. Roswell, et al., A conceptual guide to measuring species diversity, *Oikos* 130 (3) (2021) 321–338.
- [68] M. O. Hill, Diversity and evenness: A unifying notation and its consequences, *Ecology* 54 (2) (1973) 427–432.
- [69] C. E. Shannon, A mathematical theory of communication, *Bell System Tech. J.* 27 (3) (1948) 379–423.
- [70] R. Nartallo, H. Evans, E. Daly, A. Hilgers, P. Nieminen, J. Sørensen, F. Lei, P. Truscott, S. Giani, J. Apostolakis, et al., Radiation environment induced degradation on chandra and implications for xmm, *Tech. Rep. Esa/estec/tos-em/00-015/RN* (2000).
- [71] K. Morishima, M. Kuno, A. Nishio, N. Kitagawa, Y. Manabe, M. Moto, F. Takasaki, H. Fujii, K. Satoh, H. Kodama, et al., Discovery of a big void in Khufus Pyramid by observation of cosmic-ray muons, *Nature* 552 (7685) (2017) 386–390.
- [72] S. J. et al., GATE: a simulation toolkit for PET and SPECT, *Physics in Medicine & Biology* 49 (19) (2004) 4543. doi:10.1088/0031-9155/49/19/007.
- [73] CERN IT/ASD (Application Software and Databases Group), CERNLIB: short writeups, *Tech. rep.*, CERN (1996).
- [74] DD Division, The CERN Program Library, *Tech. Rep. Tech-Note-C8*, CERN (1979).
- [75] CERN Program Library, <https://cernlib.web.cern.ch/overview.html> (2003).
- [76] T. Basaglia, Z. W. Bell, D. D’Agostino, P. Dressendorfer, M. G. Pia, E. Ronchieri, Geant4 silver anniversary: 25 years enabling scientific production, *Journal of Instrumentation* 19 (01) (2024) C01037. doi:10.1088/1748-0221/19/01/C01037.
- [77] L. Carter, E. Cashwell, C. Everett, C. Forest, R. Schrandt, W. Taylor, W. Thompson, G. Turner, Monte Carlo Code Development in Los Alamos, *Tech. Rep. LA-5903-MS*, Los Alamos National Laboratory (1975).
- [78] R. L. Ford, W. R. Nelson, The EGS Code System: Computer Programs for the Monte Carlo Simulation of Electromagnetic Cascade Showers (Version 3), *Tech. Rep. SLAC-R-210*, Stanford Linear Accelerator Center (1978).
- [79] R. Brun, R. Hagelberg, M. Hansroul, J. Lassalle, Simulation program for particle physics experiments, GEANT: user guide and reference manual, *Tech. rep.*, CERN, Geneva, Switzerland (1978).
- [80] J. A. Halbleib, T. A. Mehlhorn, The Integrated TIGER Series (ITS) of Coupled Electron/Photon Monte Carlo Transport Codes, *Nuclear Science and Engineering* 92 (2) (1986) 338–339. doi:10.13182/NSE86-A18182.
- [81] Version control with Subversion, ” O’Reilly Media, Inc.”, 2008.
- [82] S. Chacon, B. Straub, Pro git, Springer, 2014.
- [83] G. Booch, Object oriented design with applications, Benjamin-Cummings Publishing Co., Inc., 1990.
- [84] D. D’Agostino, M. Pia, E. Ronchieri, Eclectic process modelling, in: 2023 IEEE Nucl. Sci. Symp., Medical Imaging Conf. and Int. Symp. Room-Temperature Semiconductor Detectors (NSS MIC RTSD), 2023. doi:10.1109/NSSMICRTSD49126.2023.10338174.
- [85] S. A. White, D. Miers, BPMN modeling and reference guide: understanding and using BPMN, Future Strategies Inc., 2008.
- [86] The Open Group, Archimate®. URL <https://www.opengroup.org/archimate-forum>
- [87] Geant4 11.2 Release Notes, <https://geant4-data.web.cern.ch/Release-Notes/ReleaseNotes.11.2.html>.
- [88] R. G. McClarren, Uncertainty quantification and predictive computational science, Springer, 2018.
- [89] M. C. Kennedy, A. O’Hagan, Bayesian calibration of computer models, *Journal of the Royal Statistical Society: Series B (Statistical Methodology)* 63 (3) (2001) 425–464. doi:https://doi.org/10.1111/1467-9868.00294.
- [90] D. E. Post, L. G. Votta, Computational Science Demands a New Paradigm, *Physics Today* 58 (1) (2005) 35–41. doi:10.1063/1.1881898.